

研究報告

Real-Time Absolute Frequency Measurement of CW-THz Wave Based on THz Combs

H26/8/4 M2 Kenta Hayashi

THz Radio Communication

Recently, THz wave has attracted attention as a new tool for high capacity radio communication



Alternative lines and backup lines for emergency

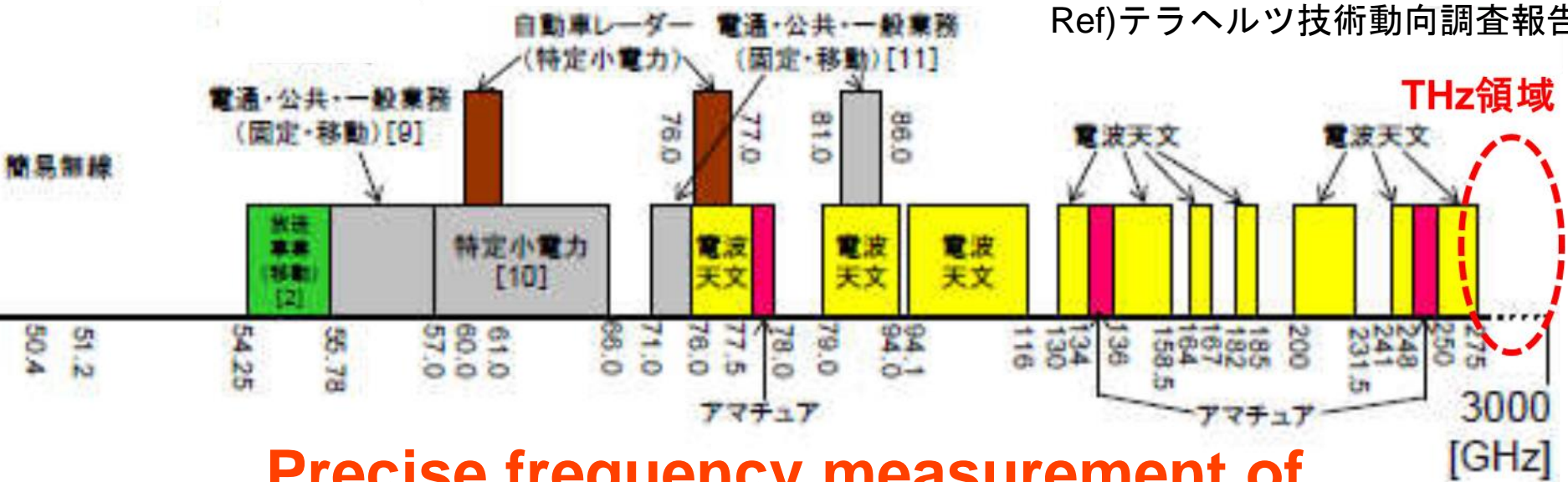


Instantaneous wireless data transfer

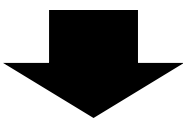
Ref)テラヘルツ波帯の情報通信利用に関する調査報告書

Frequency allocation of radio communication

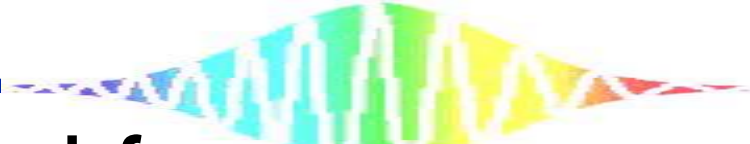
Ref) テラヘルツ技術動向調査報告



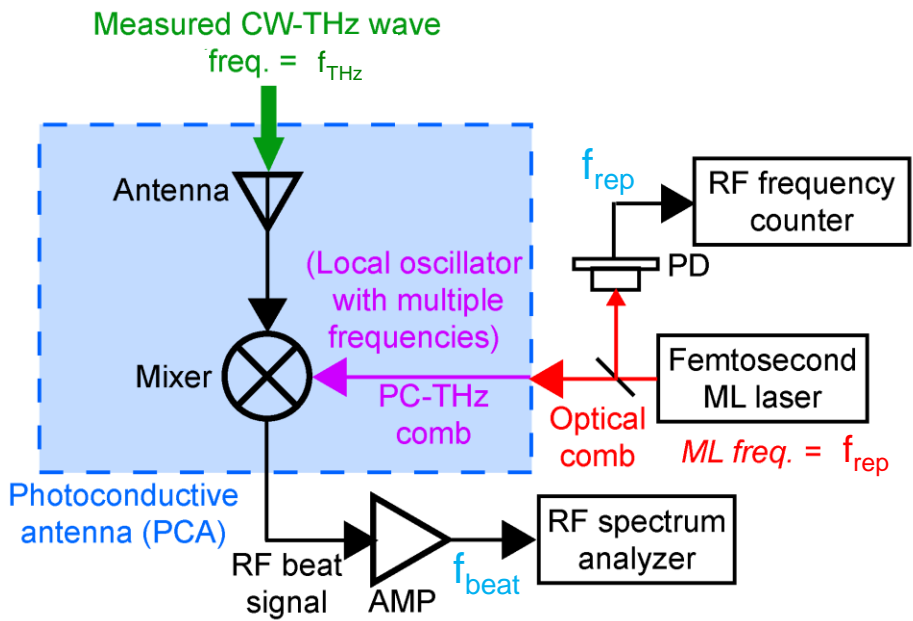
Precise frequency measurement of CW-THz wave is required



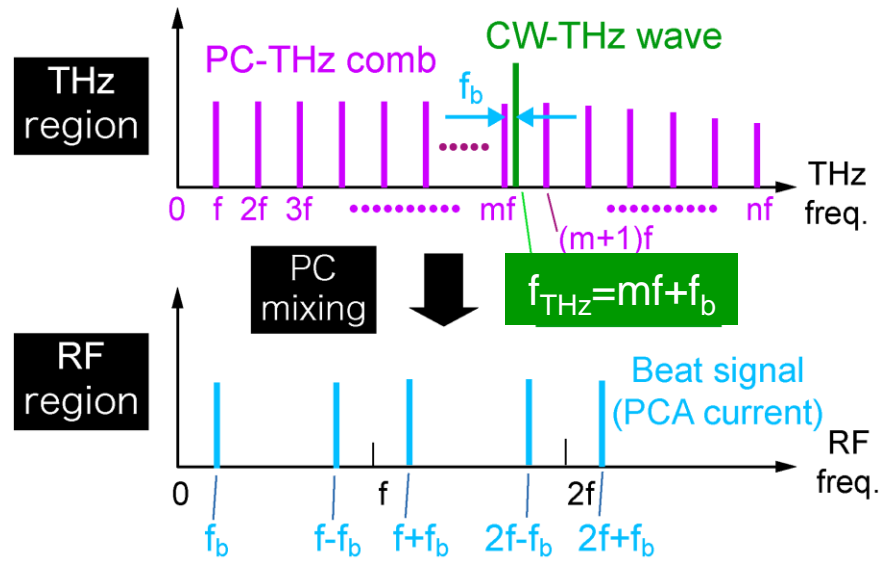
However, techniques of absolute frequency measurement of CW-THz wave are still immature!



THz-comb-referenced frequency measurement



Freq. domain

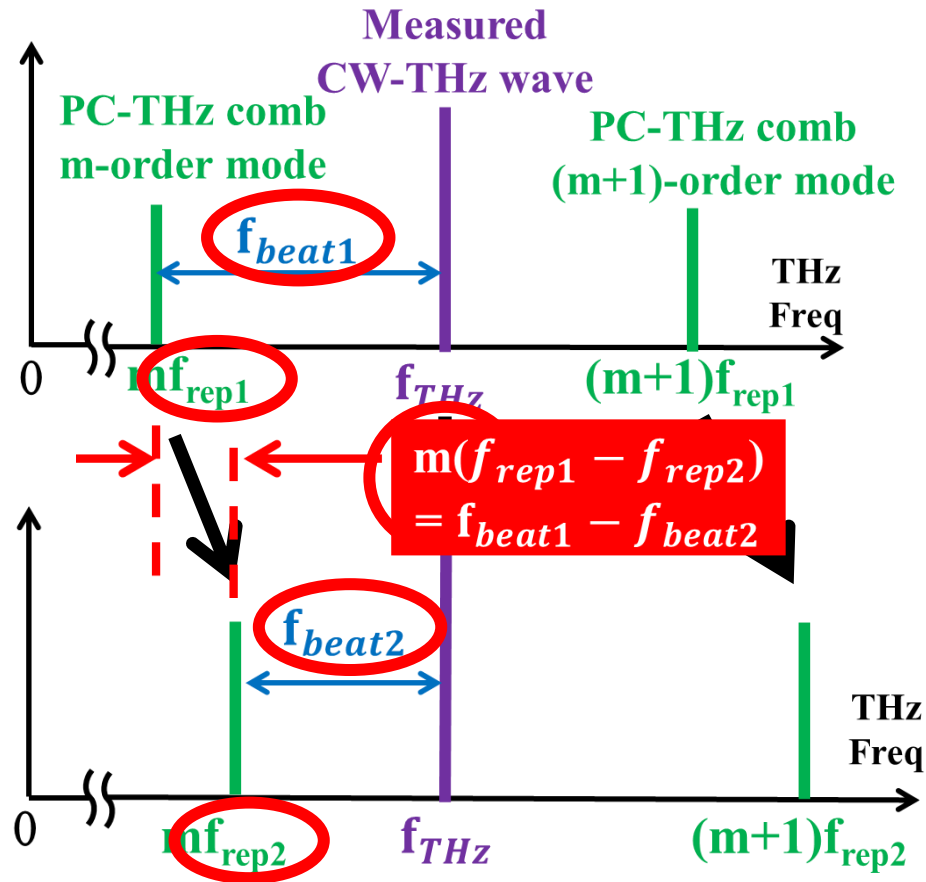


$$f_{\text{THz}} = m f_{\text{rep}} \pm f_{\text{beat}}$$

m : order of comb mode
 f_{rep} : ML frequency
 f_{beat} : beat frequency

Ref) S. Yokoyama et al, *Opt. Express* **16**, 13052-13061 (2008).
 T. Yasui et al. *Opt. Express* **17**, 17034-17043 (2009).

Determination of m and sign of f_{beat}



Measurement of f_{rep1} and f_{beat1}

$$m = \frac{|f_{beat1} - f_{beat2}|}{|f_{rep1} - f_{rep2}|}$$

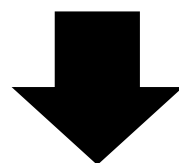
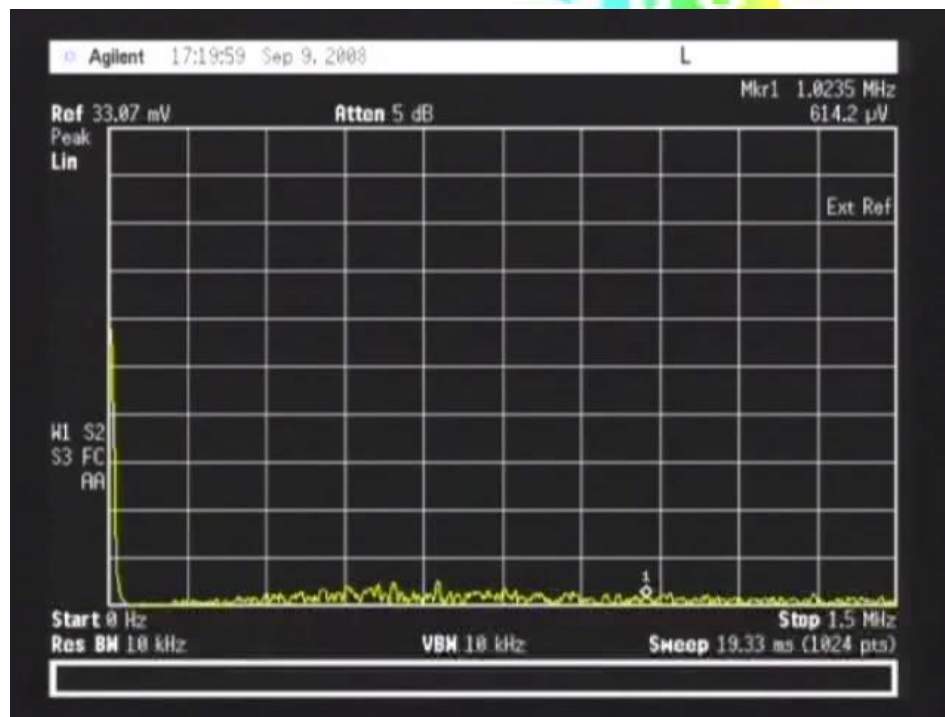
Measurement of f_{rep2} and f_{beat2}

Assumption : f_{THz} is sufficiently stable during measurements of f_{beat1} and f_{beat2}

For example

**CW-THz source
(UTC-PD)**

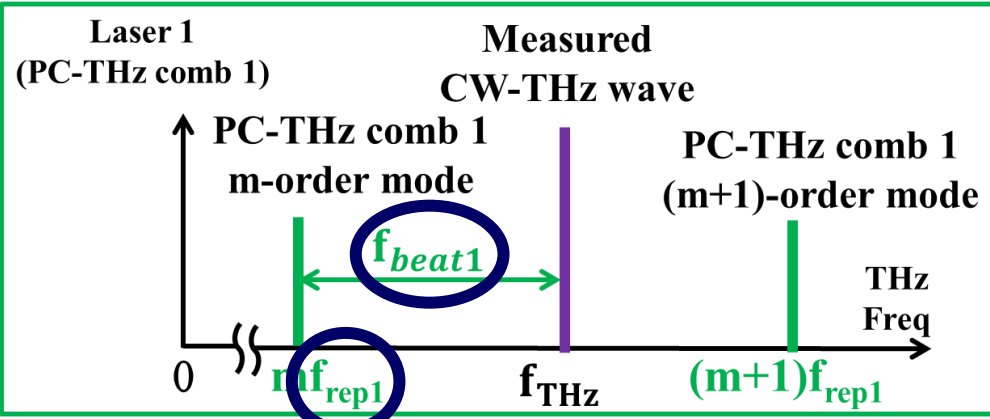
- fast frequency fluctuation
- large frequency fluctuation (mode hopping)



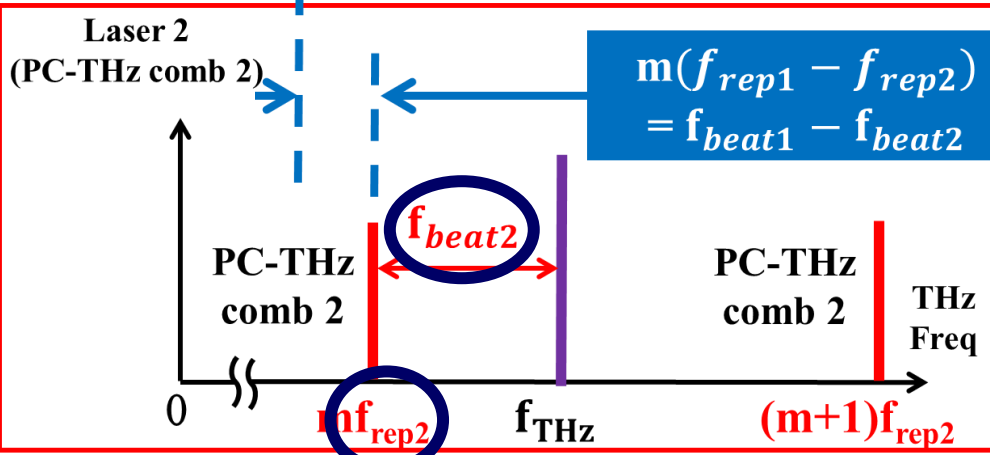
Present talk

Real-time determination of the fast or largely fluctuating CW-THz frequency using dual PC-THz combs .

Real-time determination of CW-THz frequency



parallel measurement using dual PC-THz combs !



$$m = \frac{|f_{beat1} - f_{beat2}|}{|f_{rep1} - f_{rep2}|}$$

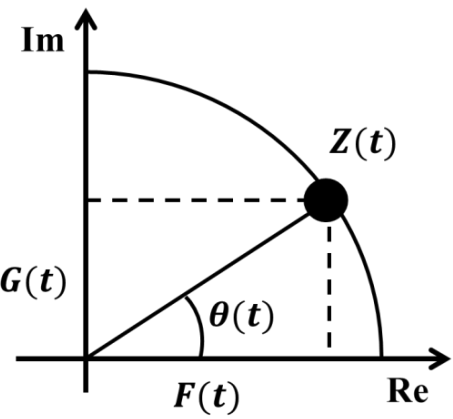
$$f_{THz} = mf_{rep1} - f_{beat1} \quad [(f_{beat1} - f_{beat2}) / (f_{rep1} - f_{rep2}) > 0]$$

$$f_{THz} = mf_{rep1} + f_{beat1} \quad [(f_{beat1} - f_{beat2}) / (f_{rep1} - f_{rep2}) < 0]$$



Instantaneous frequency measurement using Hilbert transformation

Ref) H. Fuser et al, Appl. Phys. Lett. **99**, 121111 (2011).

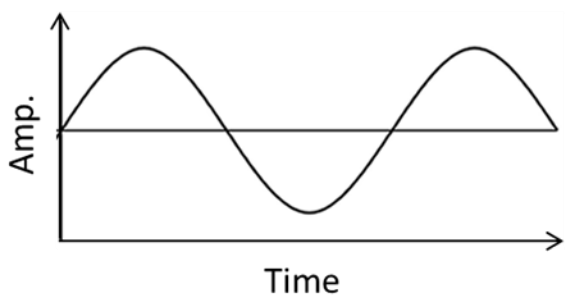


$$Z(t) = F(t) + iG(t)$$

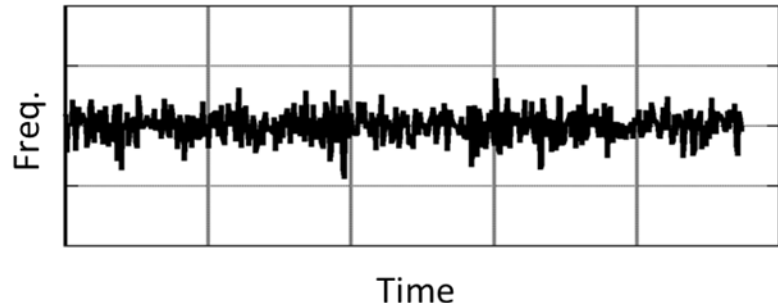
$Z(t)$: analytic signal $F(t)$: measurement signal $G(t)$: signal after Hilbert transform

$$\theta(t) = \arg[Z(t)] = \tan^{-1} \left[\frac{G(t)}{F(t)} \right]$$

$$f = \frac{1}{2\pi} \times \frac{d\theta(t)}{dt}$$

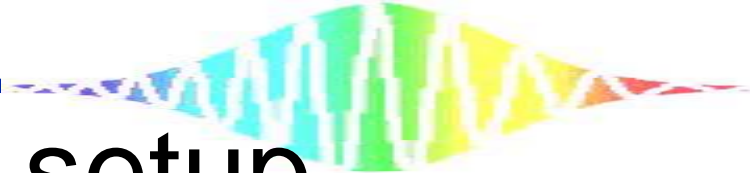


Hilbert transform

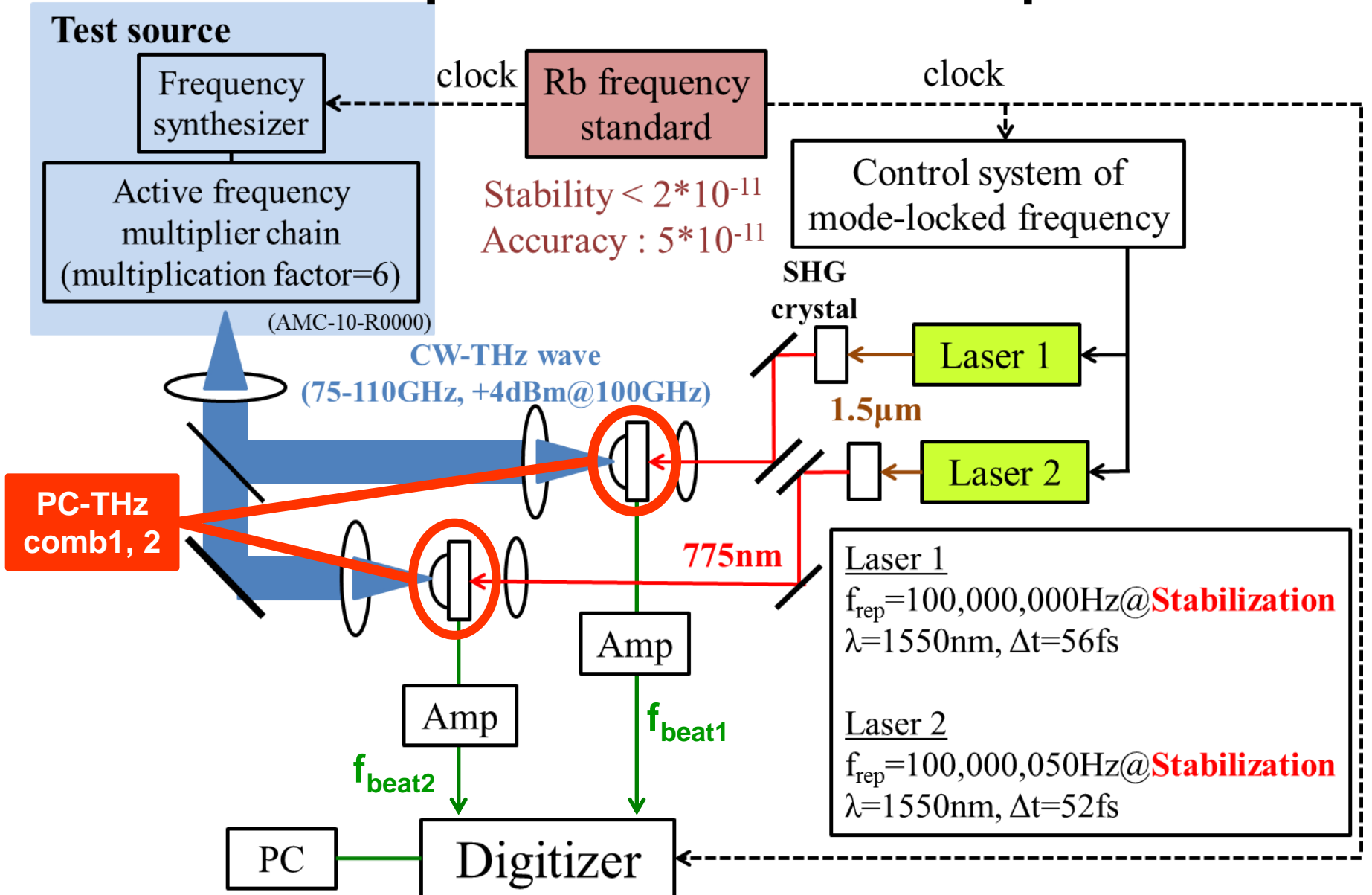


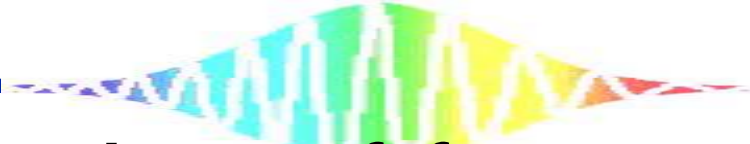
Temporal waveform of f_{beat}

Instantaneous frequency of f_{beat}



Experimental setup



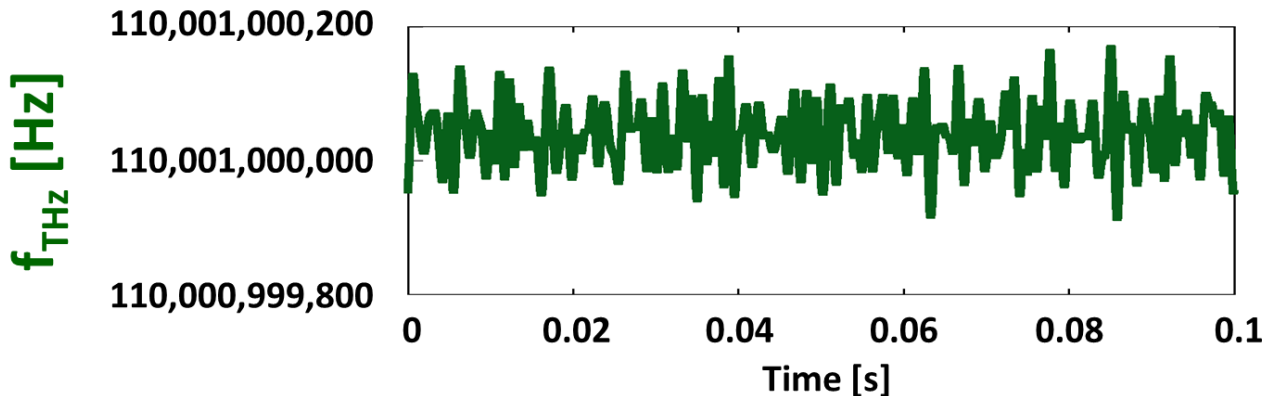
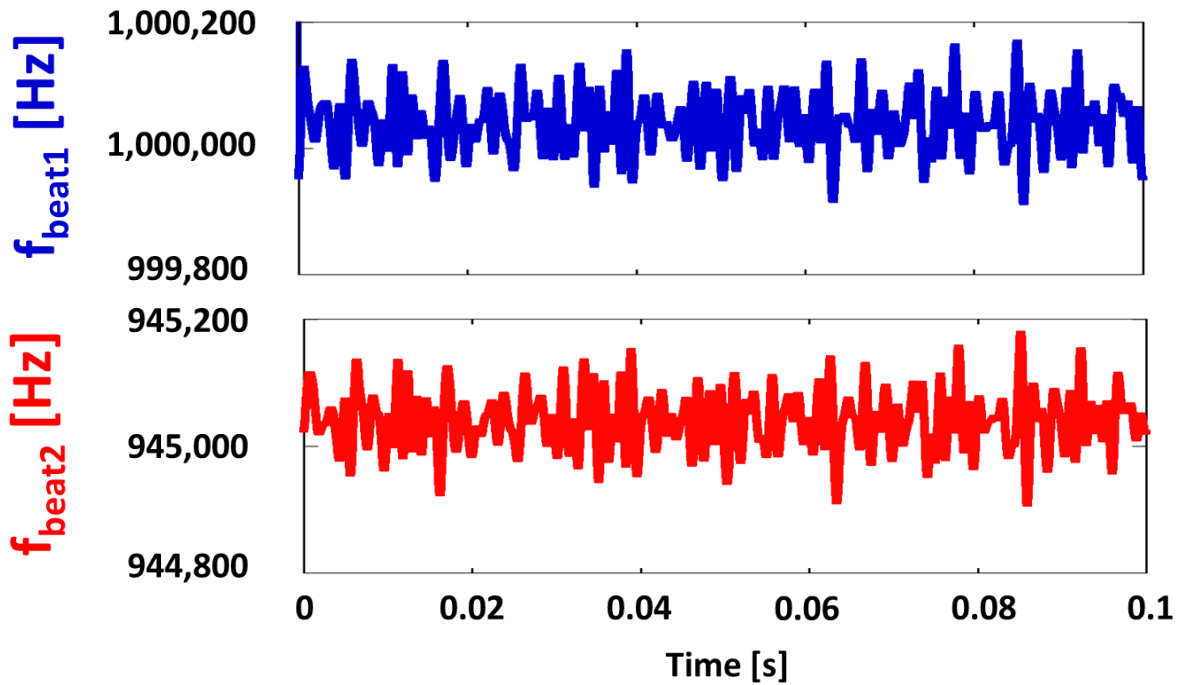


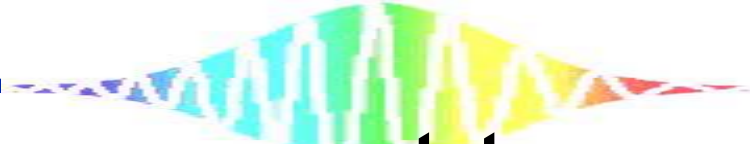
Real-time determination of f_{THz}

**Sampling rate
10MHz**

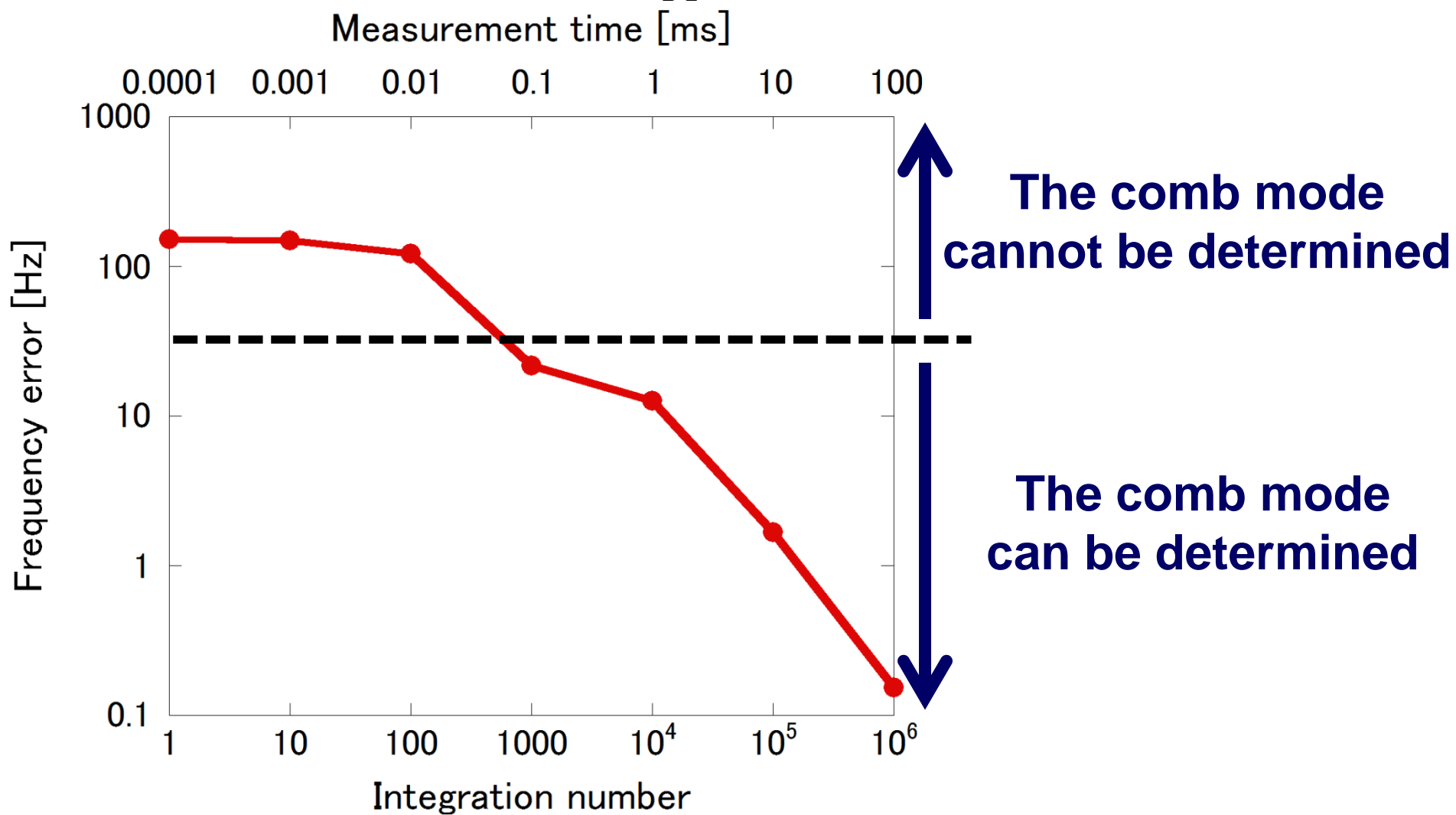
$f_{\text{rep1}} = 100,000,000 \text{ Hz}$
 $f_{\text{rep2}} = 100,000,050 \text{ Hz}$

fixed



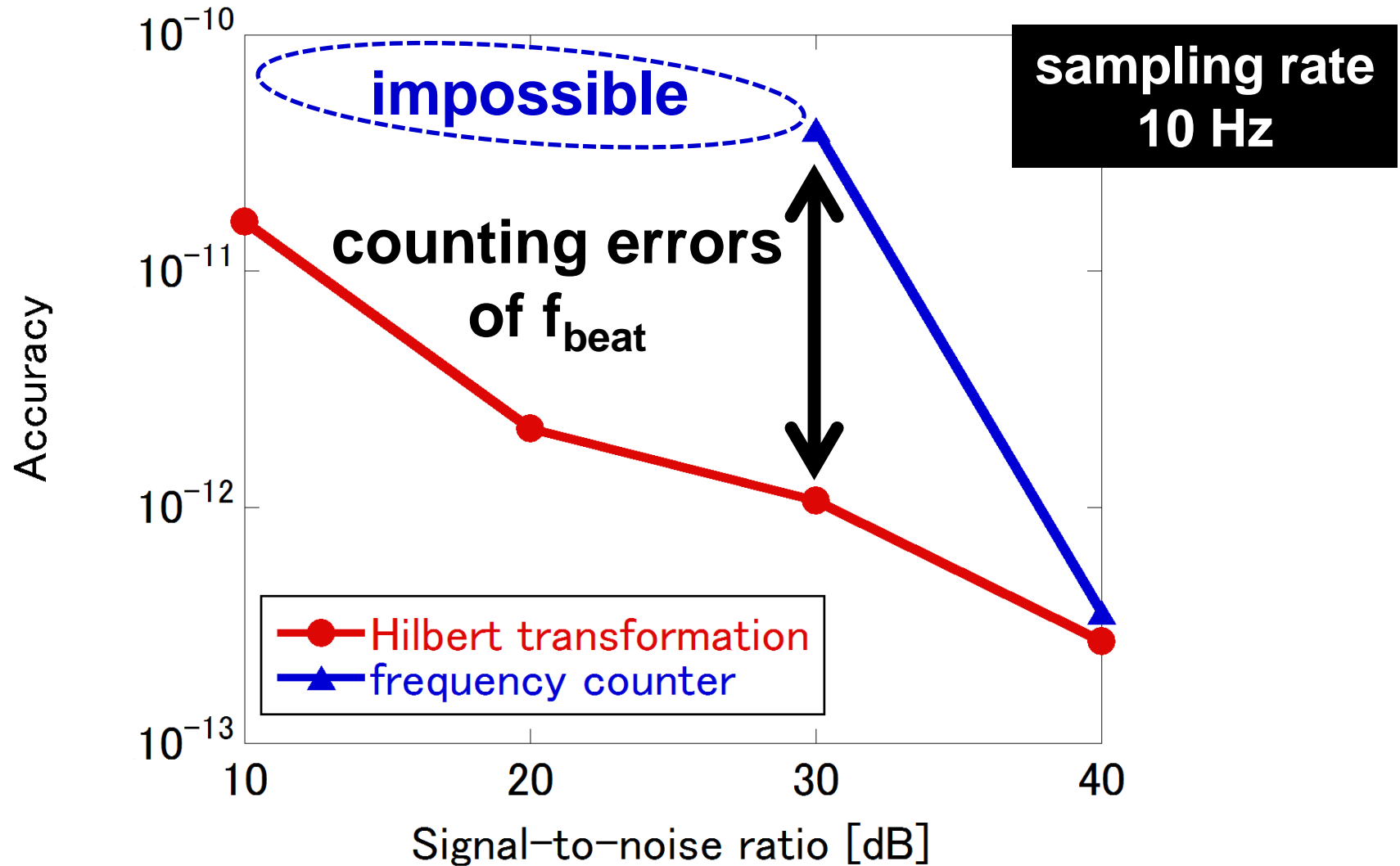


Frequency error with respect to a various integration number



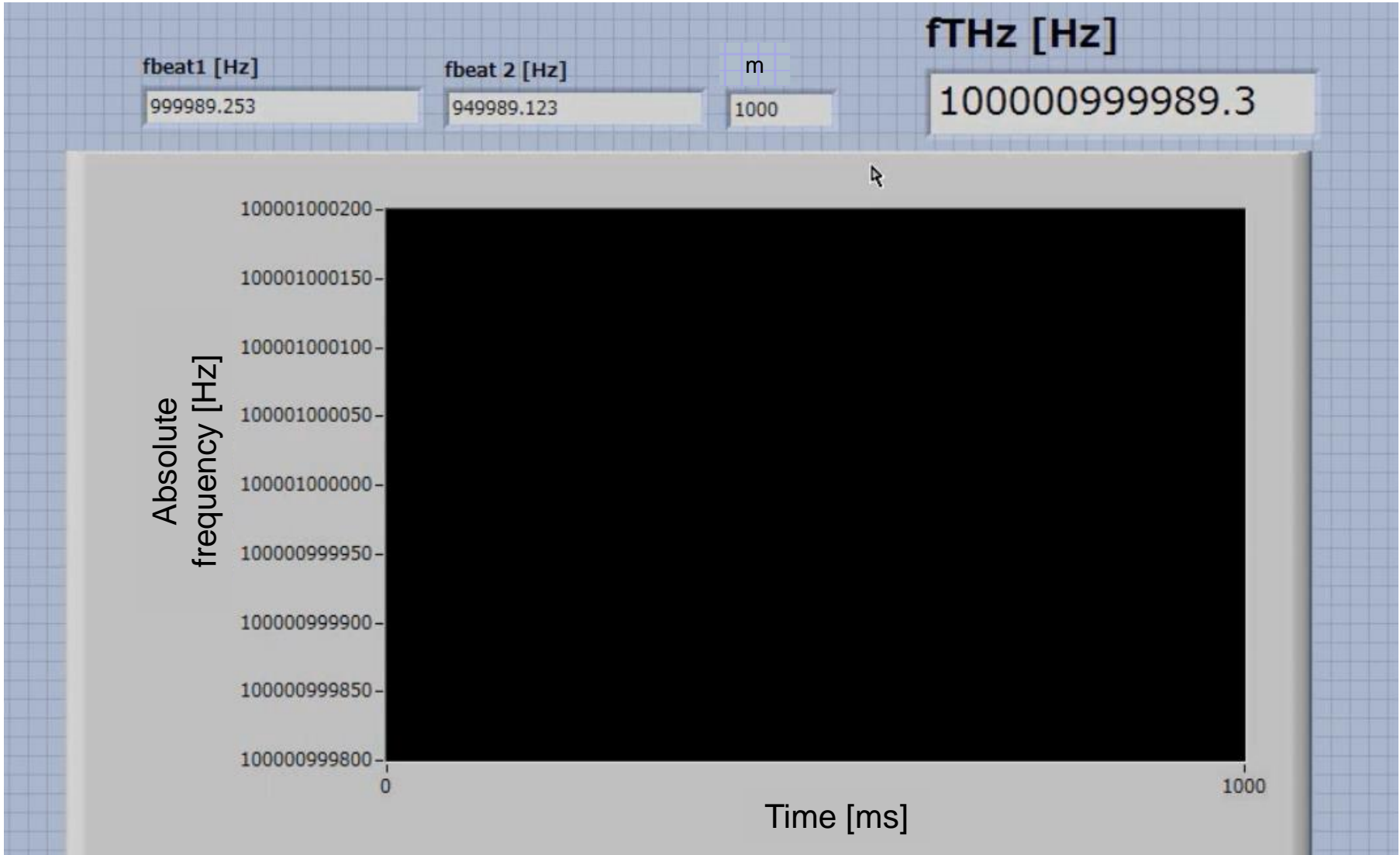


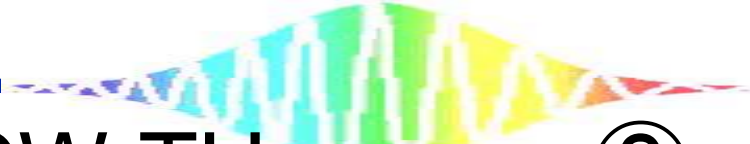
Comparison of accuracy between Hilbert transformation and frequency counter



Real-time monitoring of CW-THz wave ①

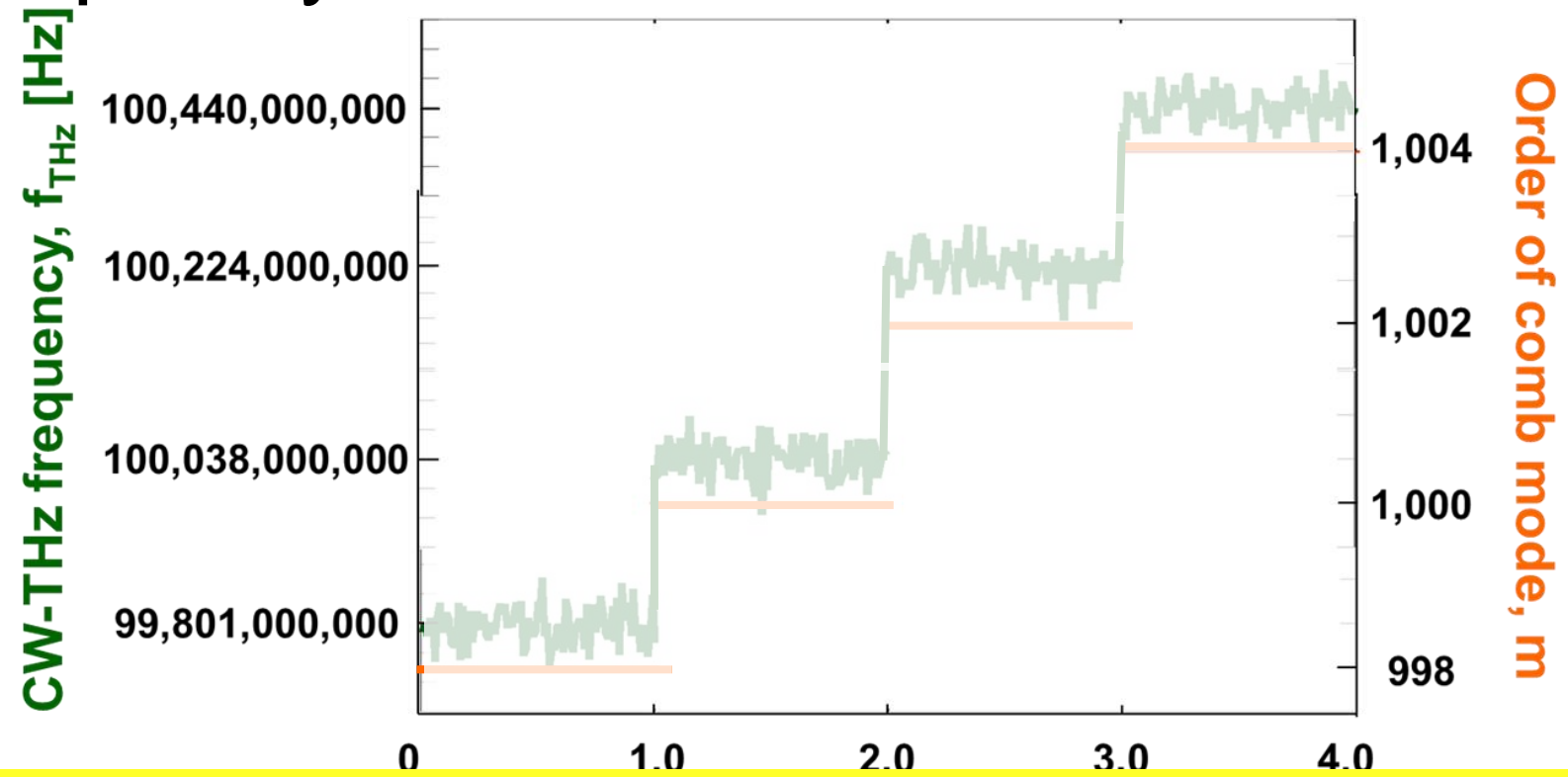
(Frequency fluctuation = 0.1 THz \pm 100 Hz)



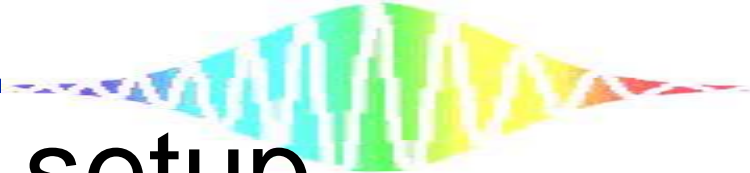


Real-time monitoring of CW-THz wave ②

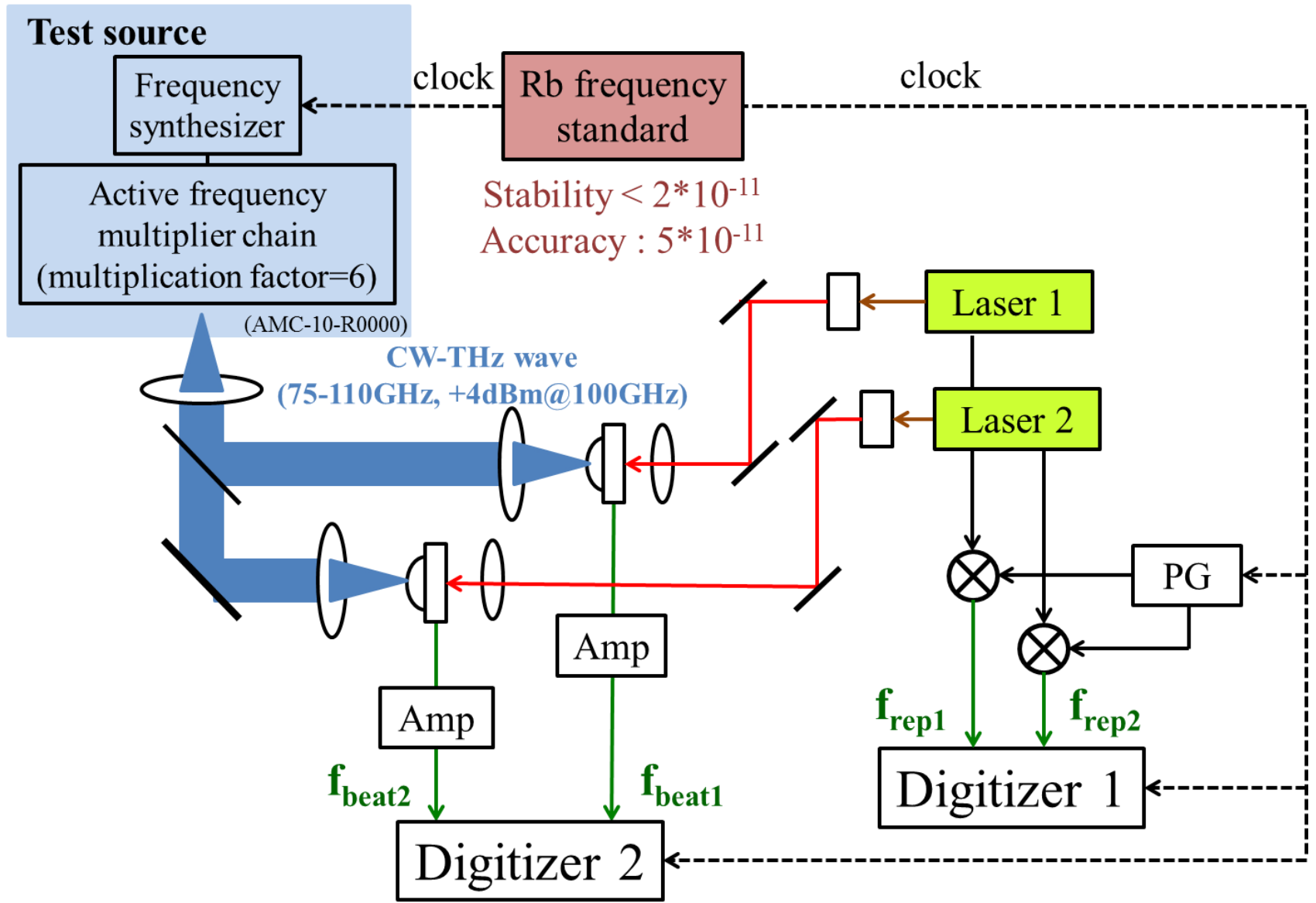
(Frequency fluctuation = 0.1THz + 200MHz)



A high potential for real time monitoring of large fluctuation such as mode hopping in CW-THz sources!



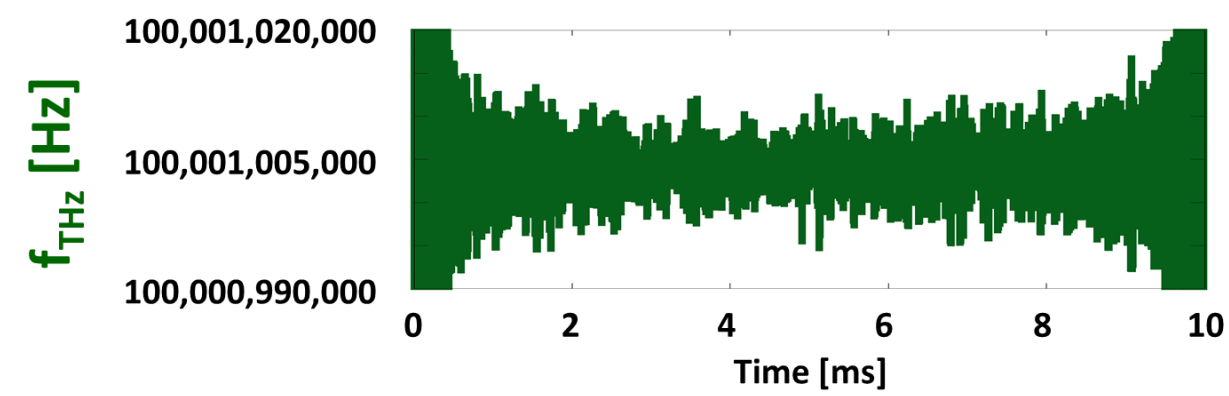
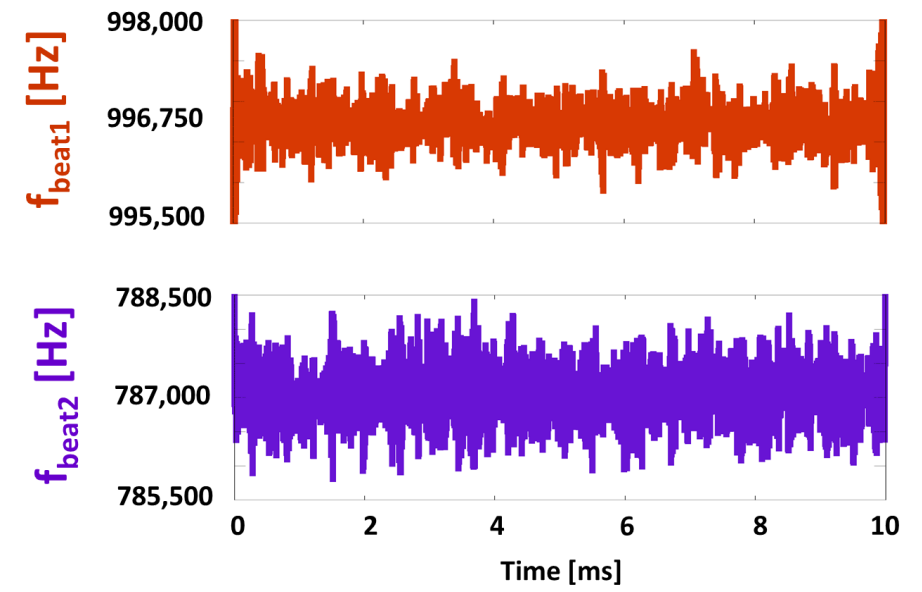
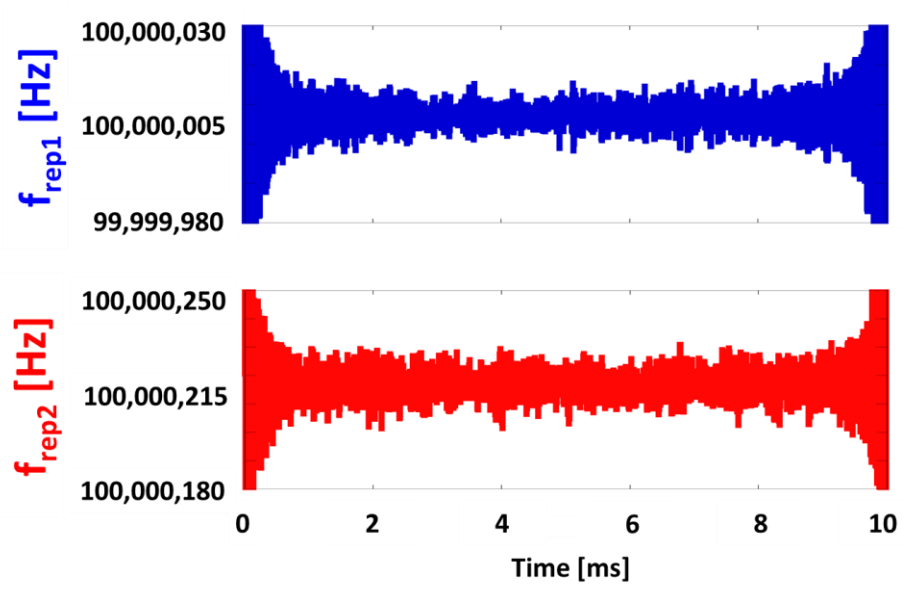
Experimental setup





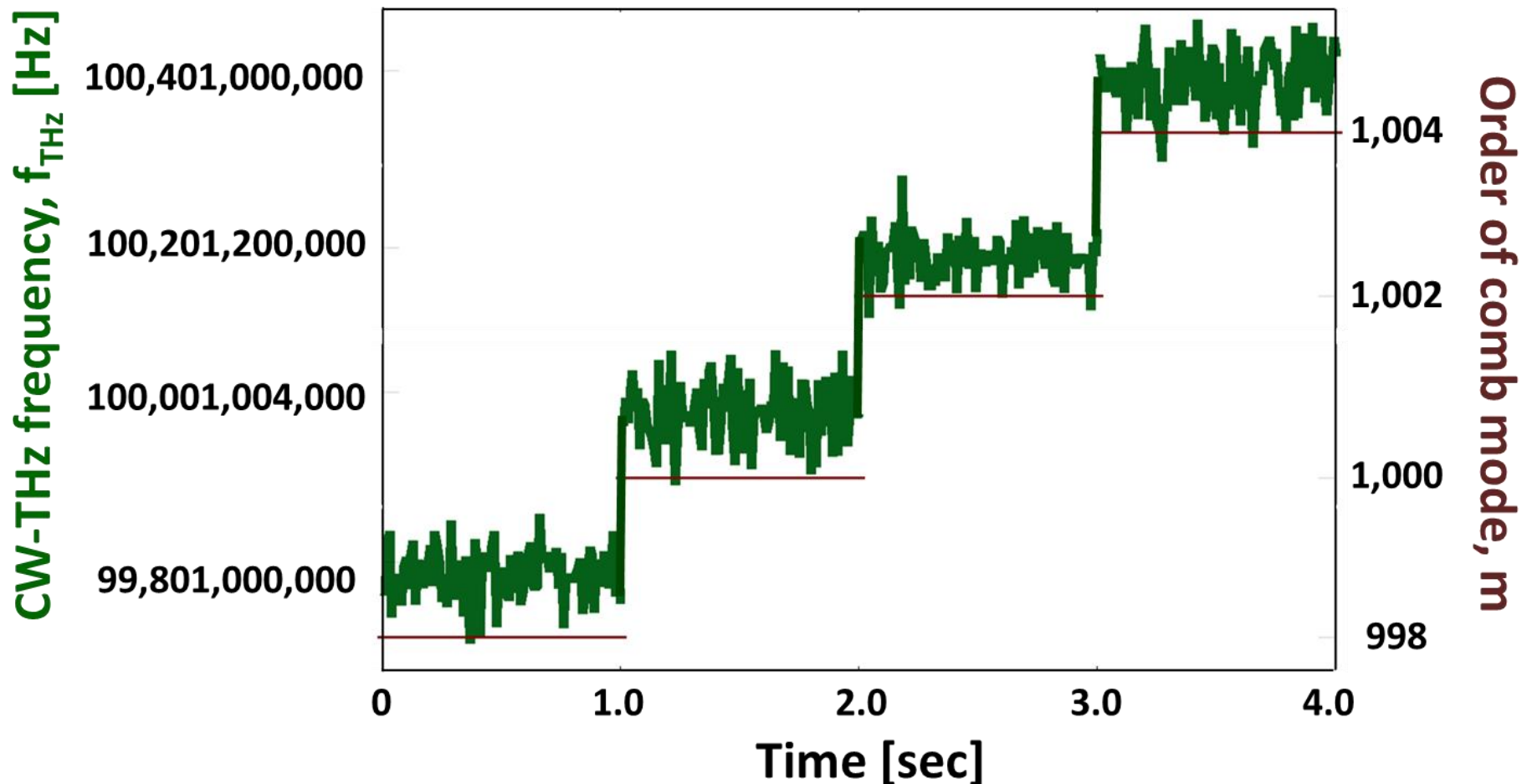
Real-time determination of f_{THz}

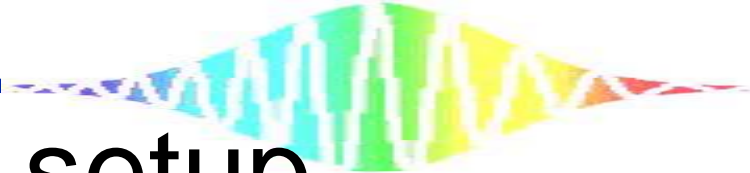
**Sampling rate
10MHz**



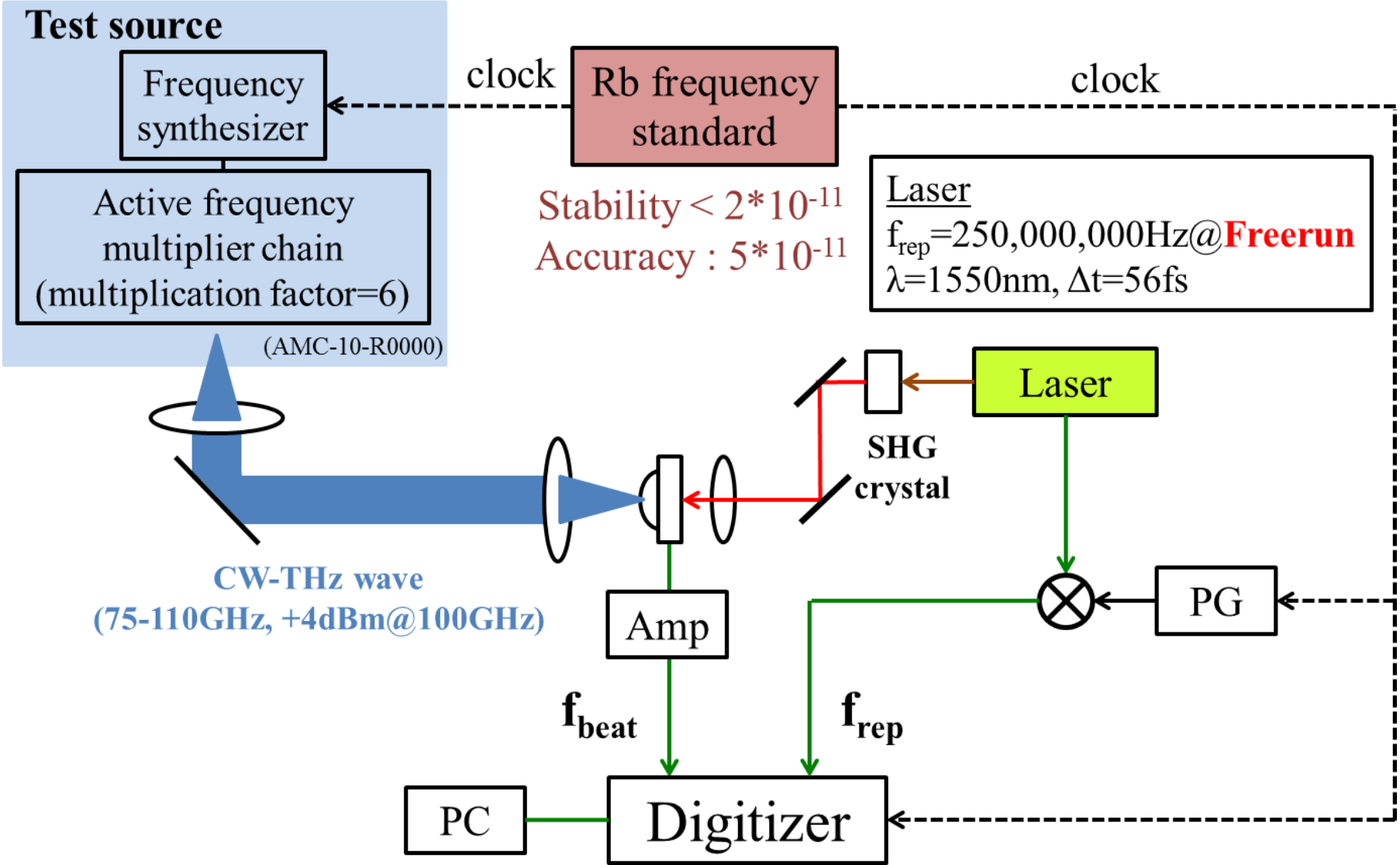


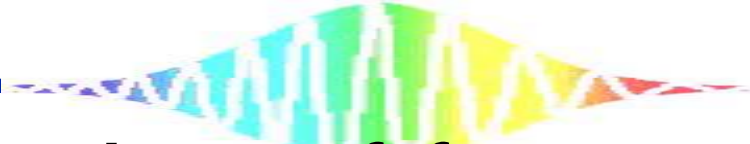
Real-time monitoring of CW-THz wave (Frequency fluctuation = 0.1THz + 200MHz)





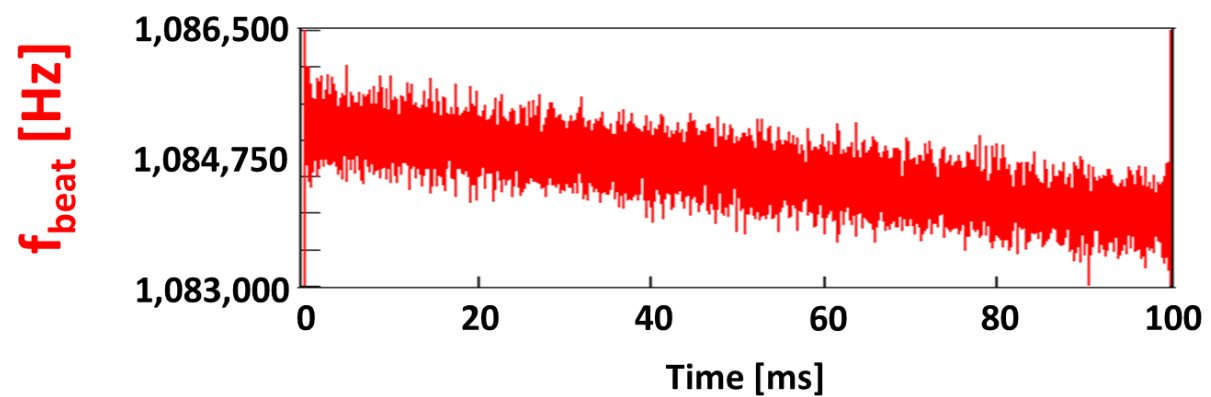
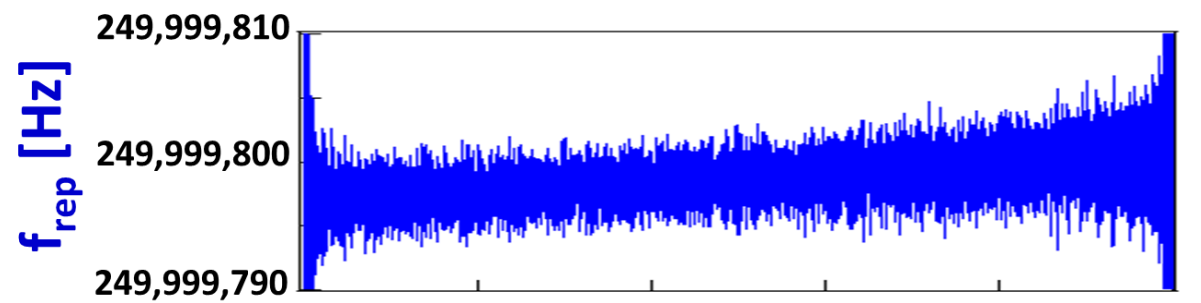
Experimental setup



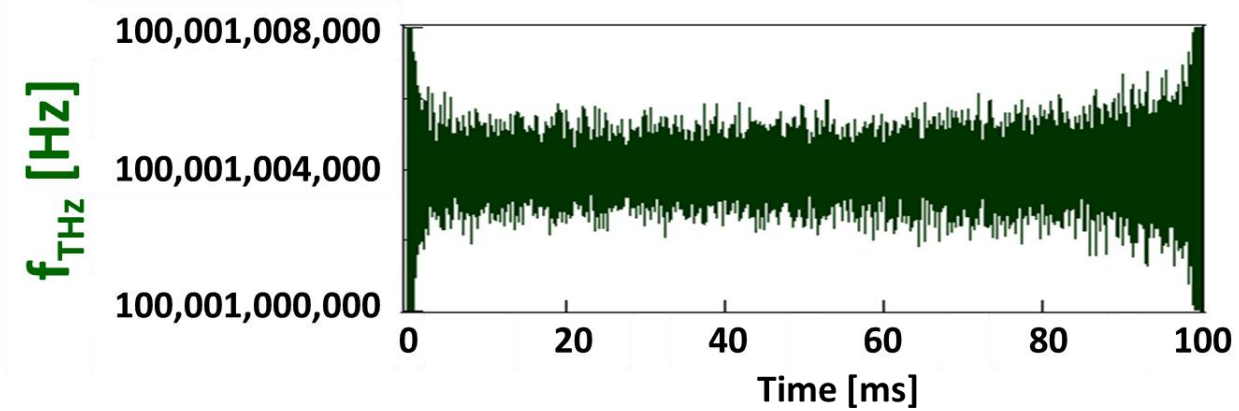


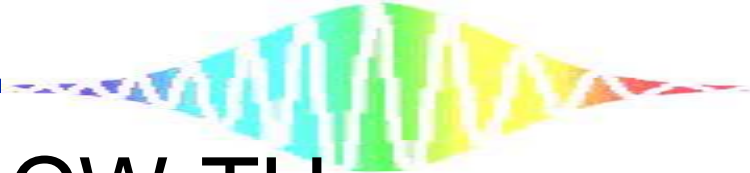
Real-time determination of f_{THz}

**Sampling rate
10MHz**

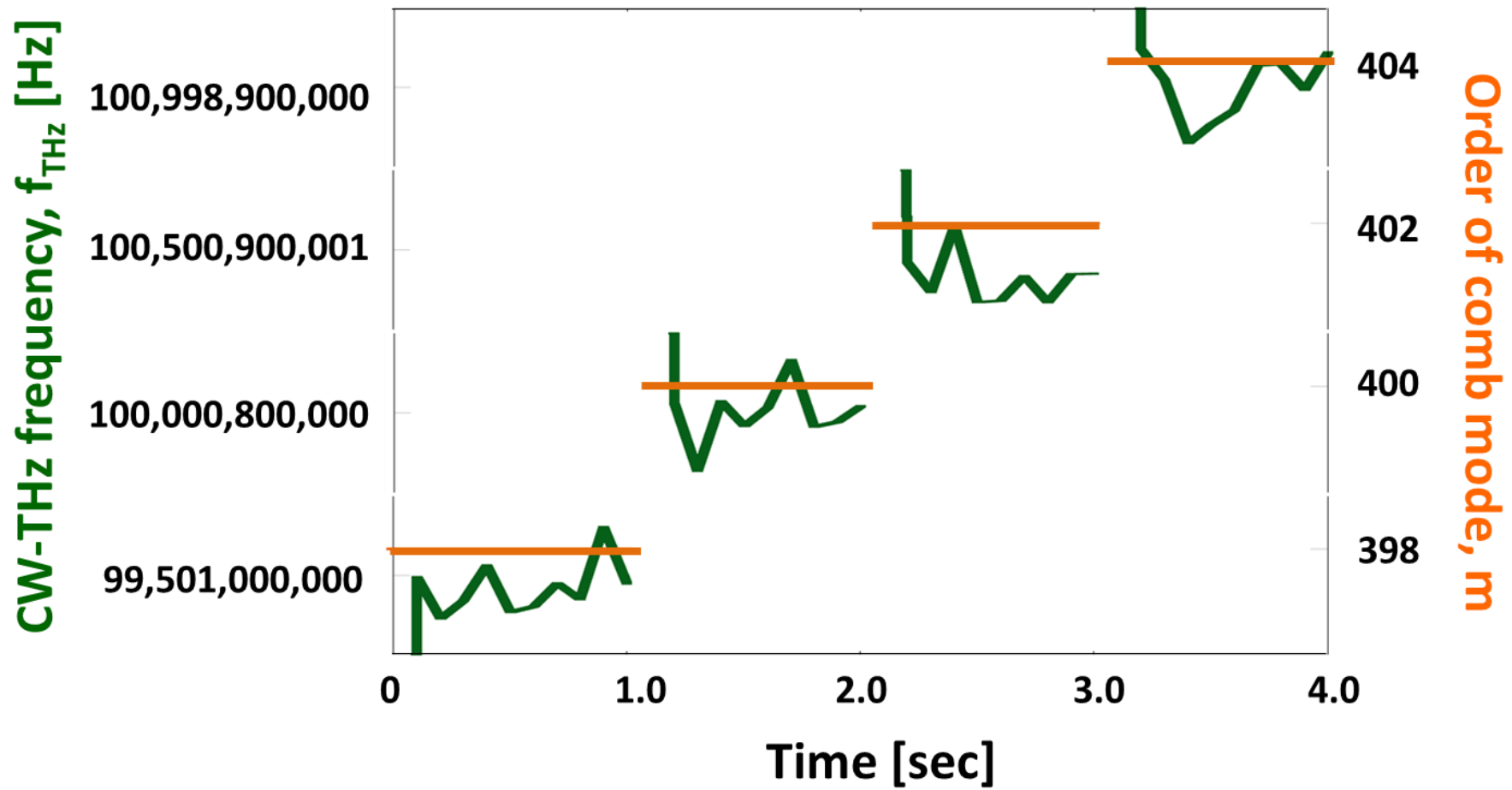


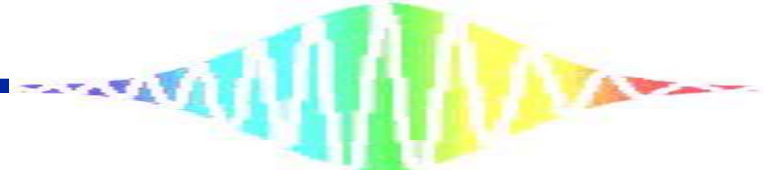
f_{rep} : freerun





Real-time monitoring of CW-THz wave (Frequency fluctuation = 0.1THz + 500MHz)





Summary

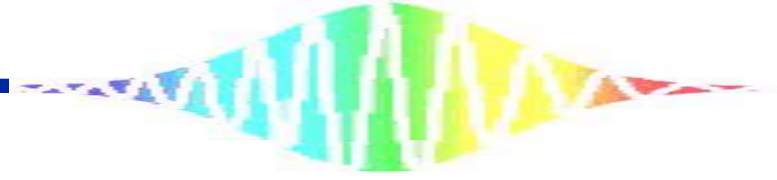
Real-time absolute frequency measurement of the fast or largely fluctuating CW-THz wave using dual PC-THz combs

(1) Frequency accuracy

- 2.2×10^{-10} at a sampling rate of 10 kHz
- 1.5×10^{-12} at a sampling rate of 10 Hz

(2) Possible to determine f_{THz} at lower SNR (~ 10)

(3) Available for large change of f_{THz} across the comb mode

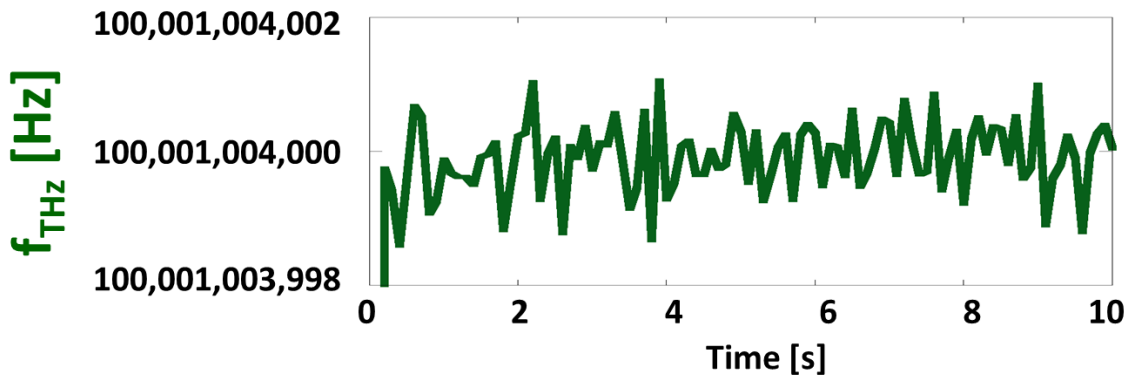
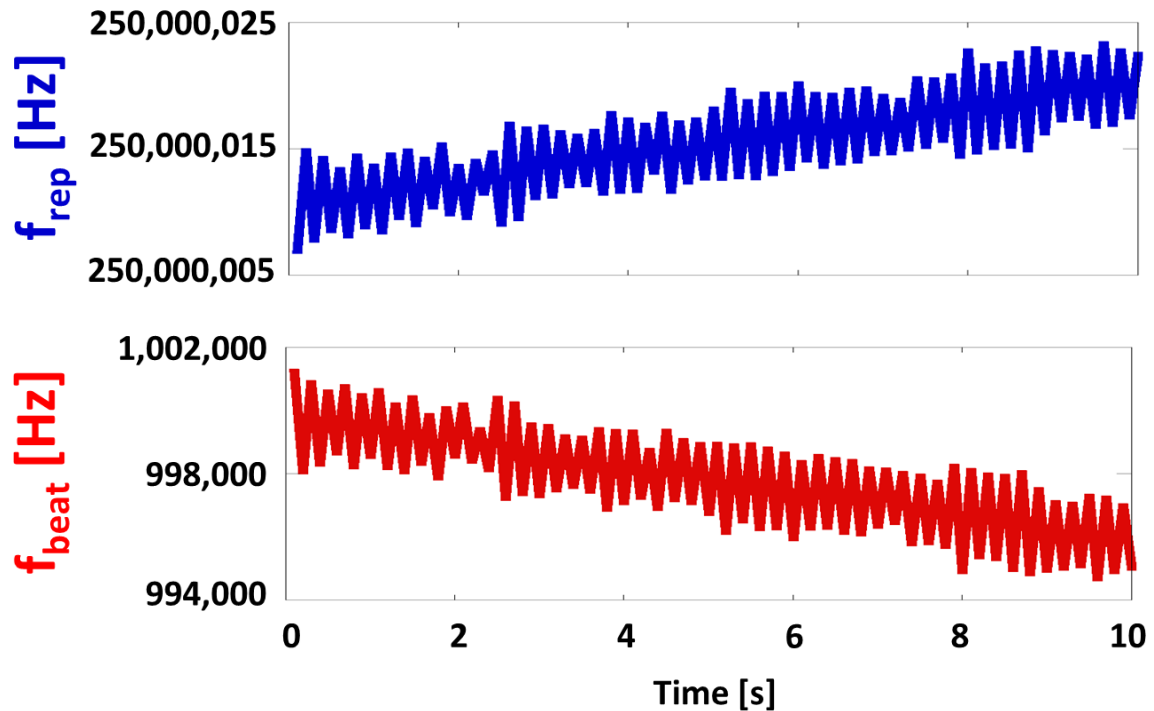




Real-time determination of f_{THz}

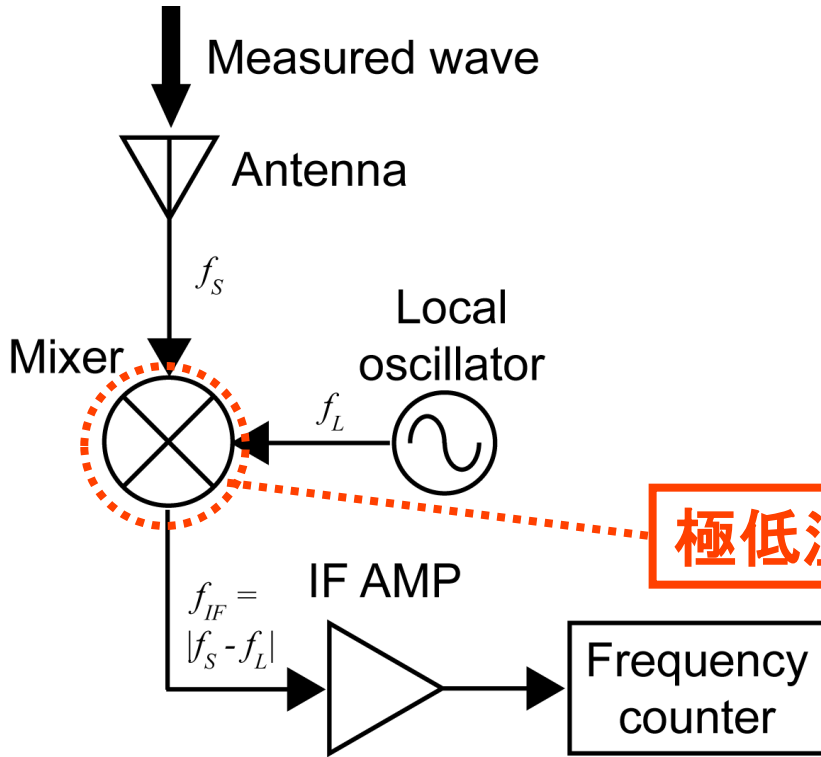
**Sampling rate
10Hz**

f_{rep} : freerun

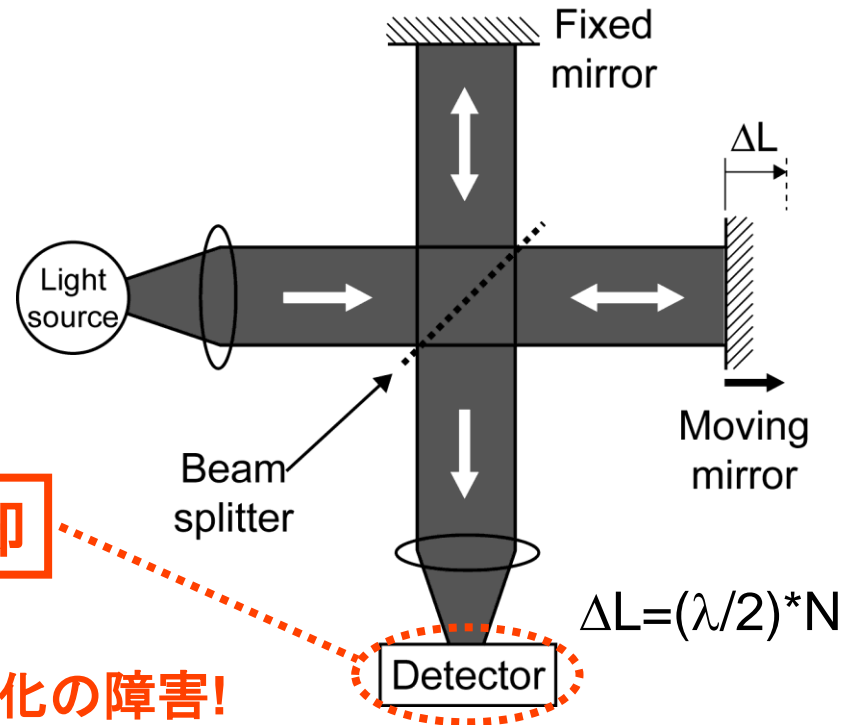


周波数計測の従来法

電気的手法 (ヘテロダイン)



光学的手法 (干渉計測)



テラヘルツ領域 (0.1~10THz) をカバーすることは難しい

→THz領域をフルカバーできる新しい手法が必要!