

Homework

H26 journal seminar

Current topic of  
Nonlinear optical microscopy

6/10 Hase

①Demirhan Kobat, Nicholas G. Horton, and Chris Xu, “In vivo two-photon microscopy to 1.6-mm depth in mouse cortex”, *Journal of Biomedical Optics* **16**, 106014 (2011).

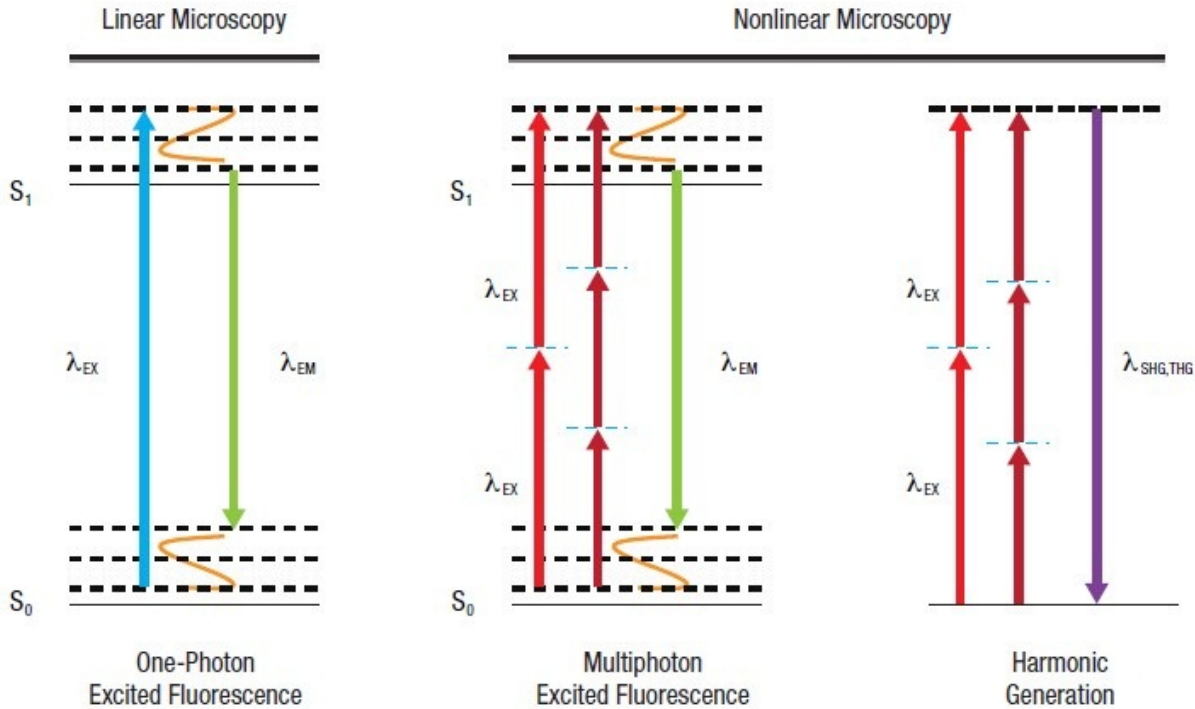
②Nicholas G. Horton, Ke Wang, Demirhan Kobat, Catharine G. Clark, Frank W. Wise, Chris B. Schaffer and Chris Xu, “In vivo three-photon microscopy of subcortical structures within an intact mouse brain”. *Nature Photonics* **20**, 1 (2013).

③Adrian F. Pegoraro, Aaron D. Slepko, Andrew Ridsdale, Douglas J. Moffatt and Albert Stolow, “Hyperspectral multimodal CARS microscopy in the fingerprint region”. *Journal of Biophotonics* **7**, 49 (2014).

# Homework

- Spatial resolution of
  - Two Photon Fluorescence
  - Three Photon Fluorescence
- Spectral focussing CARS

# Multi Photon Fluorescence



<http://www.thorlabs.com>

- Two Photon absorption

$$\frac{dI(z)}{dz} = -\frac{3\omega}{2n_0^2 c^2 \epsilon_0} \chi_I^{(3)}(-\omega; \omega, -\omega, \omega) I(z)^2 \quad \alpha_2 = \frac{3\omega}{2n_0^2 c^2 \epsilon_0} \chi_I^{(3)}(-\omega; \omega, -\omega, \omega)$$

$$\frac{dI(z)}{dz} = -\alpha_2 I(z)^2$$

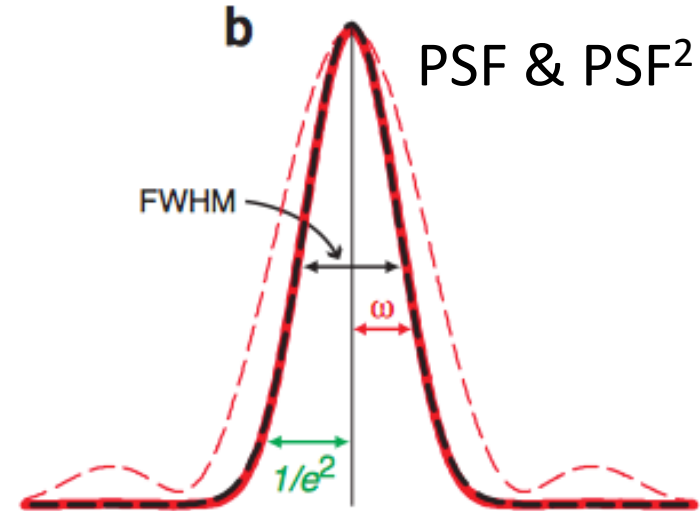
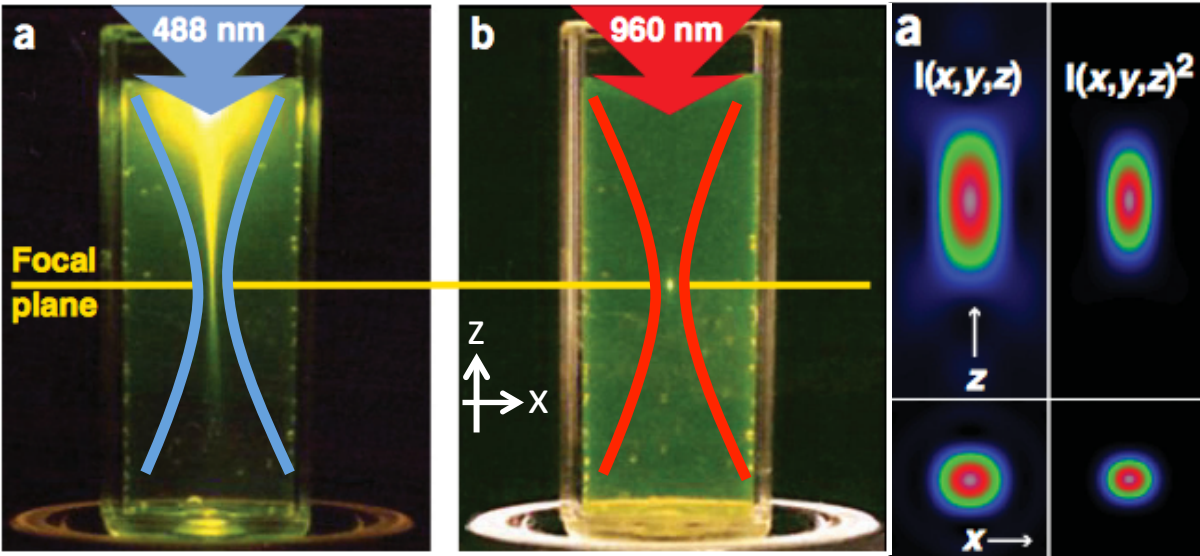
- Three Photon absorption

$$\frac{dI(z)}{dz} = -\frac{5\omega}{2n_0^3 c^3 \epsilon_0^2} \chi_I^{(5)}(-\omega; \omega, -\omega, \omega, -\omega, \omega) I(z)^3 = -\alpha_3 I(z)^3 \quad \alpha_3 = \frac{5\omega}{2n_0^3 c^3 \epsilon_0^2} \chi_I^{(5)}(-\omega; \omega, -\omega, \omega, -\omega, \omega)$$

# Spatial resolution

One Photon

Two Photon



$$\text{PSF}_{\text{one-photon}} = \text{PSF}(v, u)$$

$$\text{PSF}_{\text{confocal}} = \text{PSF}_{\text{illumination}} \times \text{PSF}_{\text{detection}} \approx \text{PSF}^2(v, u)$$

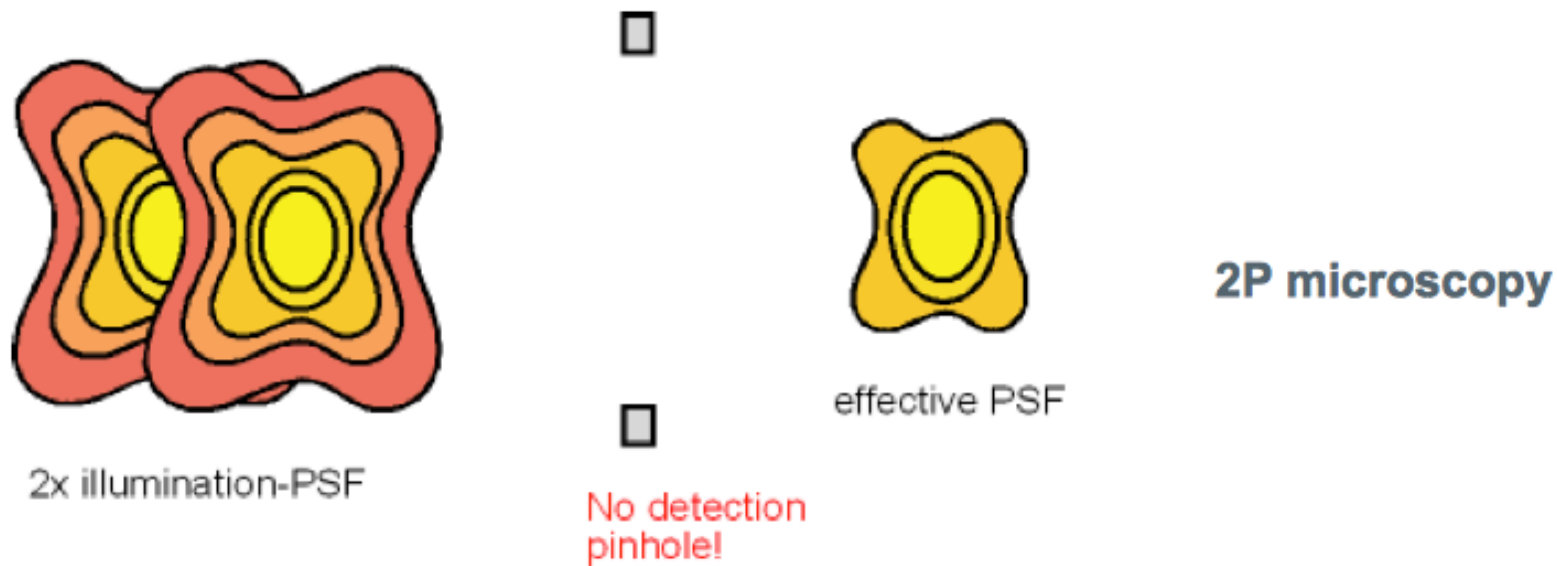
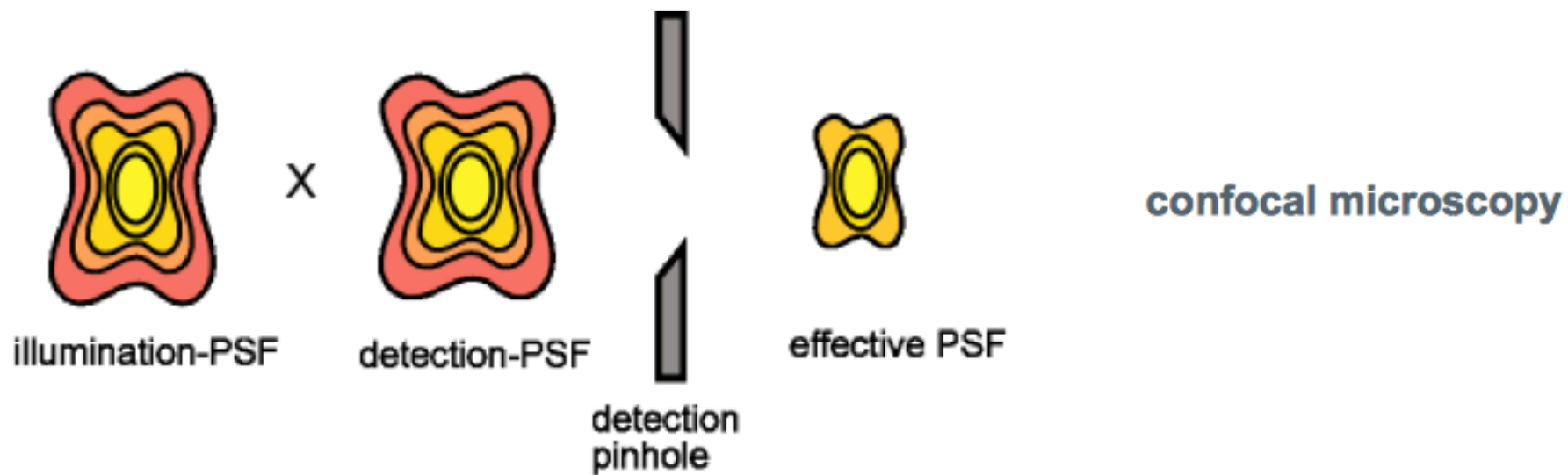
$$\text{PSF}_{\text{two-photon}} = (\text{PSF}_{\text{illumination}})^2 \approx \text{PSF}^2(v/2, u/2)$$

$$\text{PSF}_{\text{Three-photon}} = (\text{PSF}_{\text{illumination}})^3 = \text{PSF}^3(v/3, u/3)$$

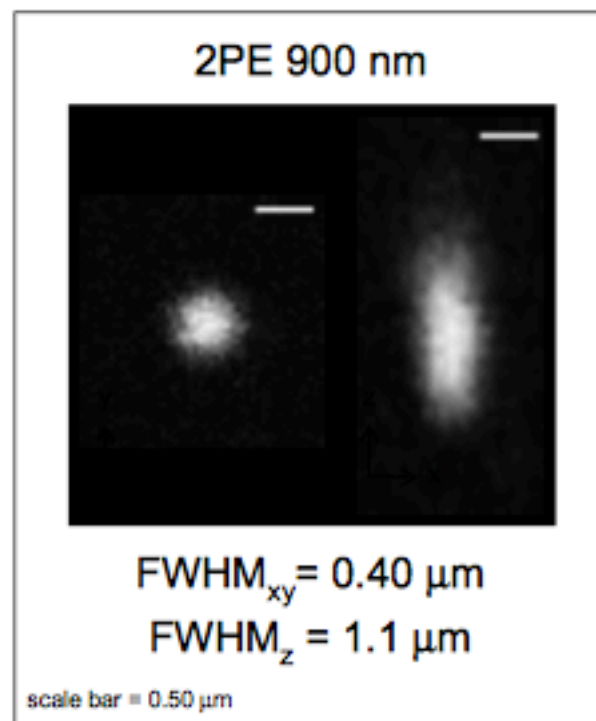
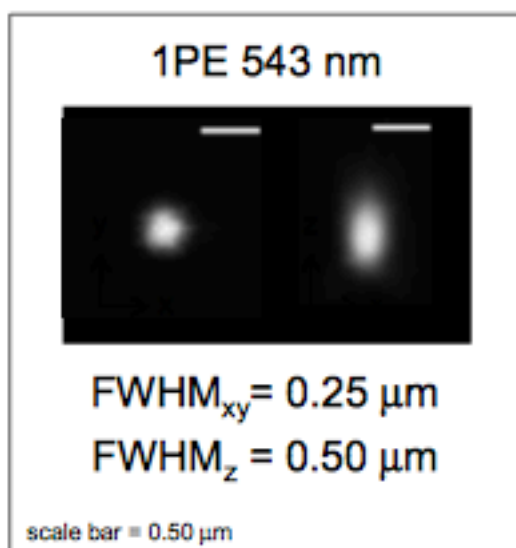
$$v = k (\text{NA}) r \quad k = 2\pi/\lambda$$

$$u = k (\text{NA})^2 z$$

radial and axial  
normalized coordinates



# Resolution in multiphoton microscopy



**Orange bead ( $\varnothing 0.18 \mu\text{m}$ ) imaged with 60x/1.4 oil objective**

Table 11.1. Comparison of resolution between two-photon and three-photon fluorescence microscopy under the condition of the equal fluorescence wavelength,  $v$  and  $u$  are normalized by the fluorescence wavelength.  $v_{1/2}$  and  $u_{1/2}$  are the transverse half widths at half maximum of the 3-D IPSP.  $\Delta u_{1/2}$  is the half width at half maximum for an axial response to a thin layer,  $\gamma$  the gradient of the image intensity at surface of a thick layer,  $\gamma'$  the gradient of the image intensity at the edge of a thin layer, and  $\gamma''$  the gradient of the image intensity at the edge of a thick edge

		Conventional (1-photon)	Confocal (1-photon)	Conventional (2-photon)	Confocal (2-photon)	Conventional (3-photon)	Confocal (3-photon)
width of IPSP	$v_{1/2}$	1.62	1.17	2.34	1.34	2.86	1.41
	$u_{1/2}$	5.56	4.01	8.02	4.62	9.87	4.89
	$\Delta u_{1/2}$	$\infty$	4.3	8.6	5.1	9.98	5.67
axial resolution	$\gamma$	0	0.09	0.045	0.093	0.047	0.082
	$\gamma'$	0.27	0.417	0.208	0.361	0.171	0.349
transverse resolution	$\gamma''$	0	0.333	0.167	0.340	0.166	0.305

Table 11.2. Comparison of resolution between two-photon and three-photon fluorescence microscopy under the condition of the equal illumination wavelength,  $v$  and  $u$  are normalized by the incident wavelength. The others conditions are the same those in Table 11.1

		Conventional (1-photon)	Confocal (1-photon)	Conventional (2-photon)	Confocal (2-photon)	Conventional (3-photon)	Confocal (3-photon)
lateral resolution	$v_{1/2}$	0.81	0.58	1.17	0.67	0.953	0.47
	$u_{1/2}$	2.78	2.0	4.01	2.31	3.29	1.63
axial resolution	$\Delta u_{1/2}$	$\infty$	2.15	4.3	2.50	3.33	1.89
	$\gamma$	0	0.18	0.09	0.186	0.141	0.246
transverse resolution	$\gamma'$	0.54	0.84	0.416	0.722	0.513	1.047
	$\gamma''$	0	0.67	0.334	0.68	0.498	0.915



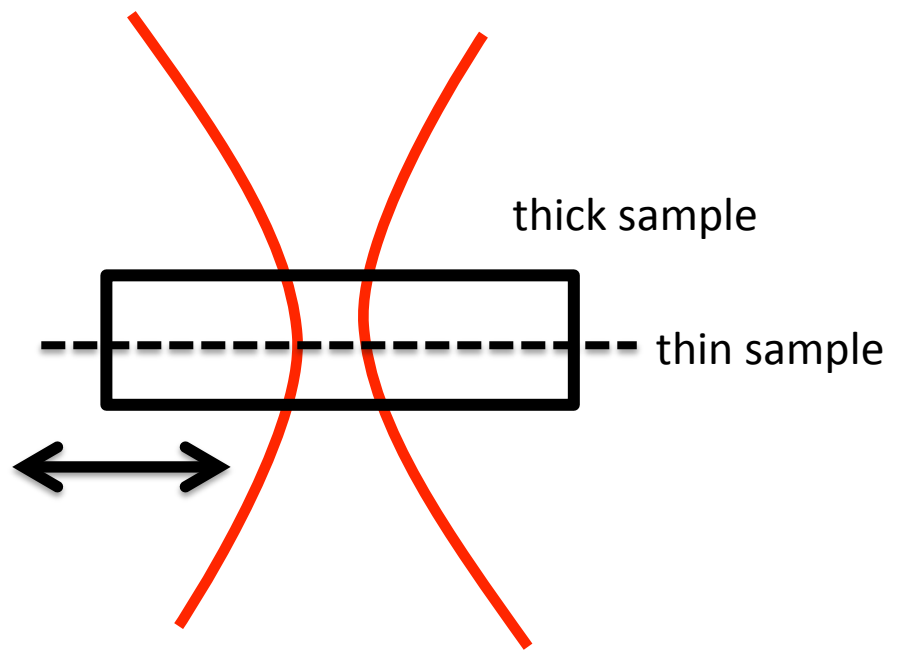
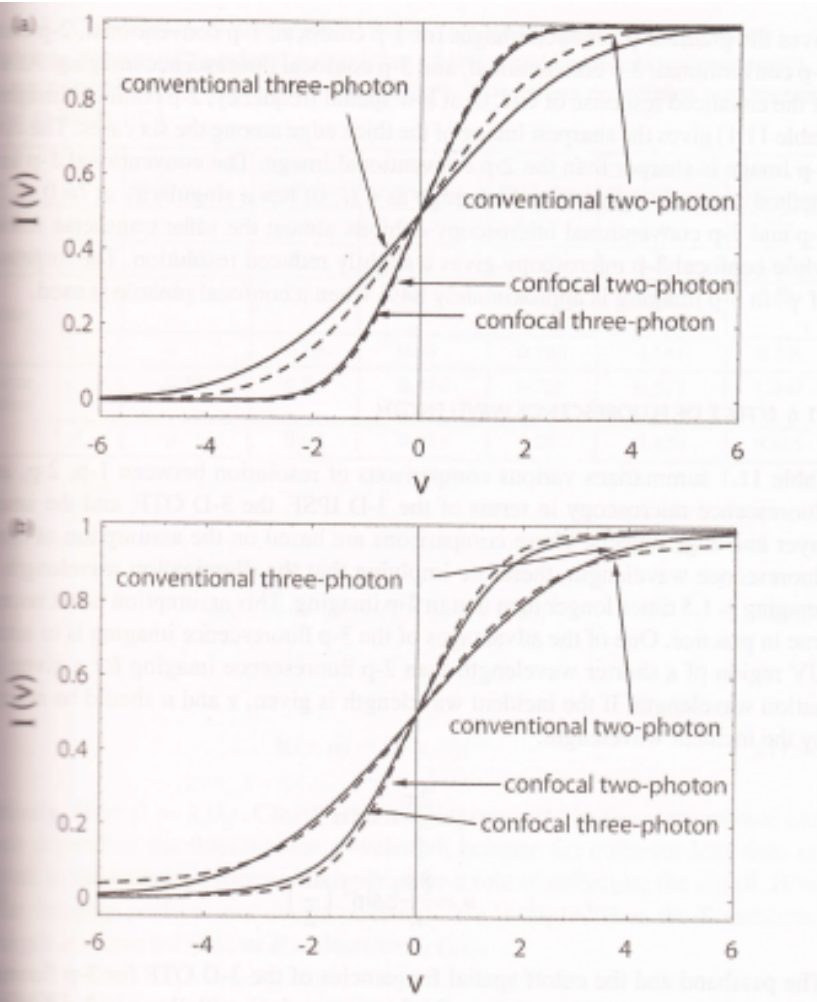


Figure 11.5. Image intensity of thin (a) and thick (b) fluorescent edges. The other figures are the same as those in Figure 11.1.

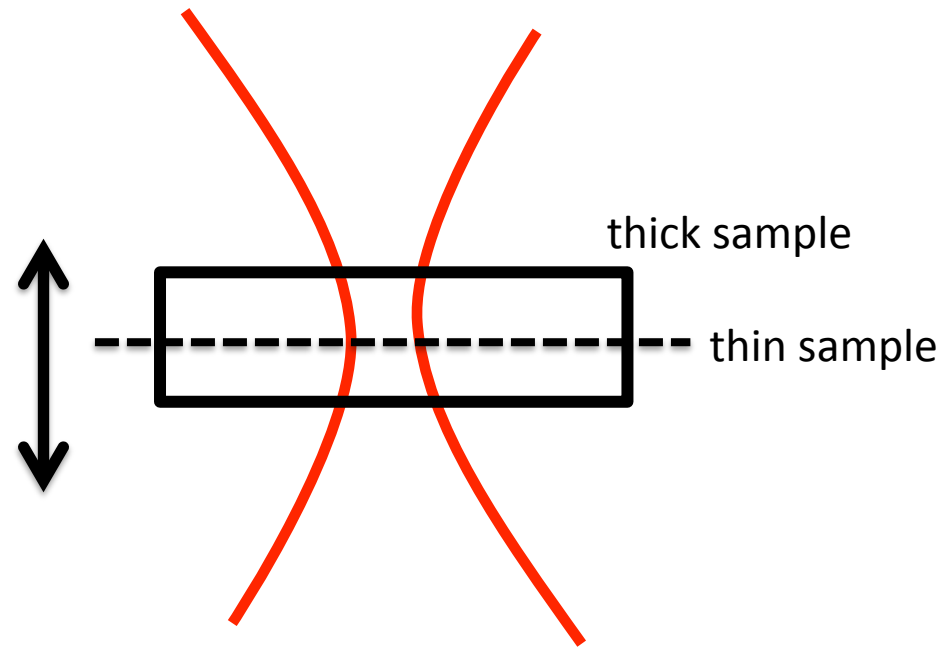
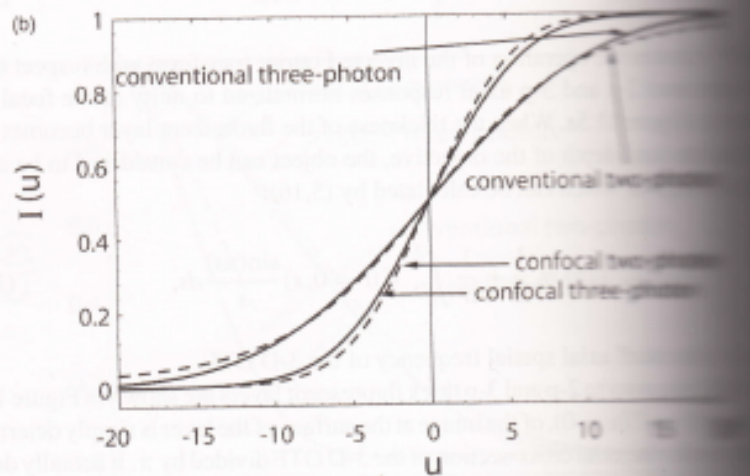
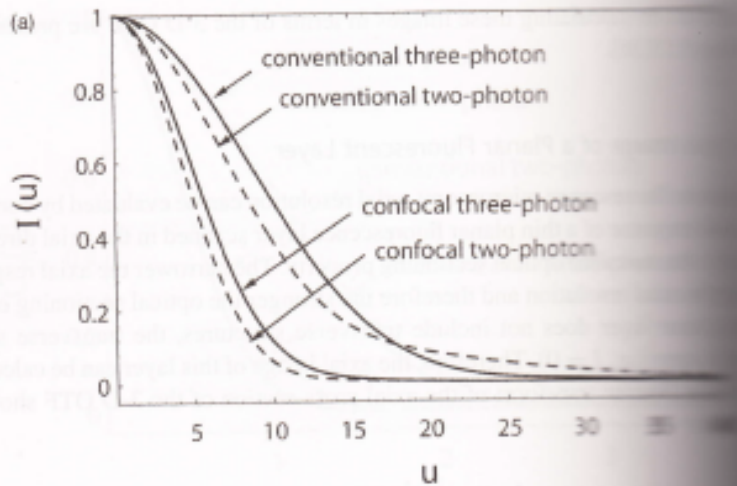
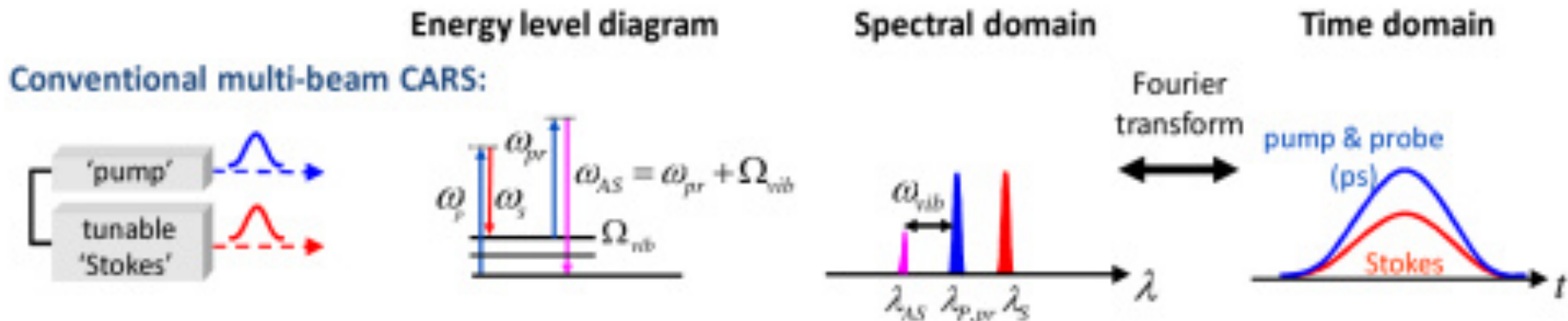
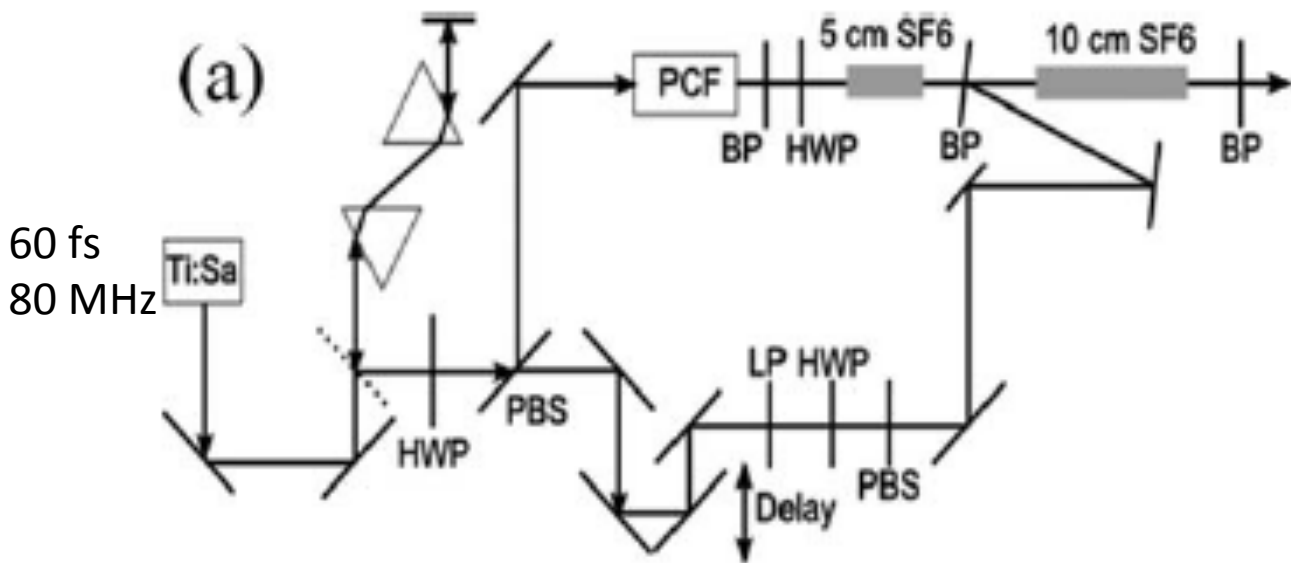
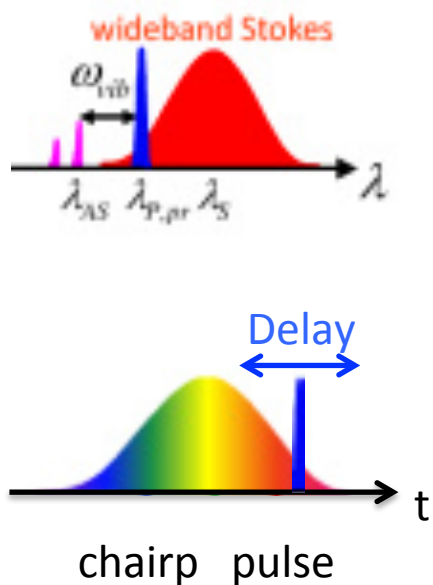


Figure 11.5. Image intensity of thin (a) and thick (b) fluorescent layers. The same conditions are the same as those in Figure 11.1.

# Spectral focussing CARS



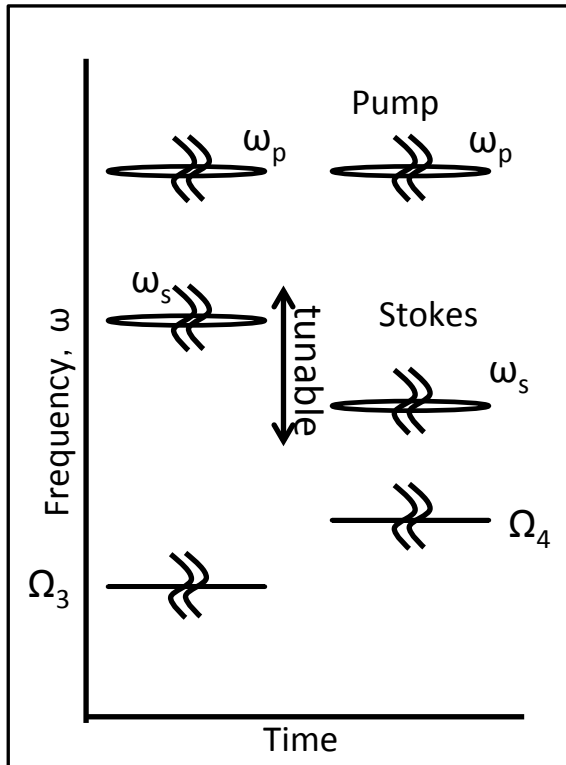
This paper



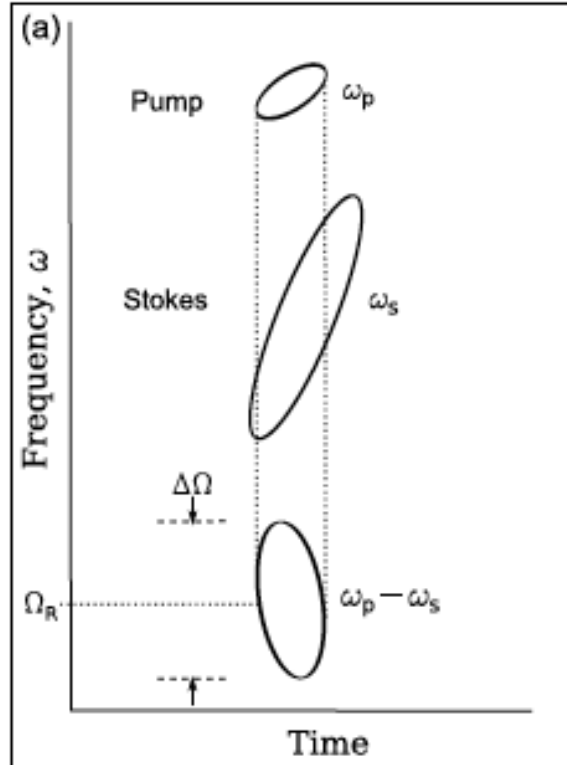
# Spectral focussing CARS

Raman active vibrational mode:  $\omega_p - \omega_s = \Omega$

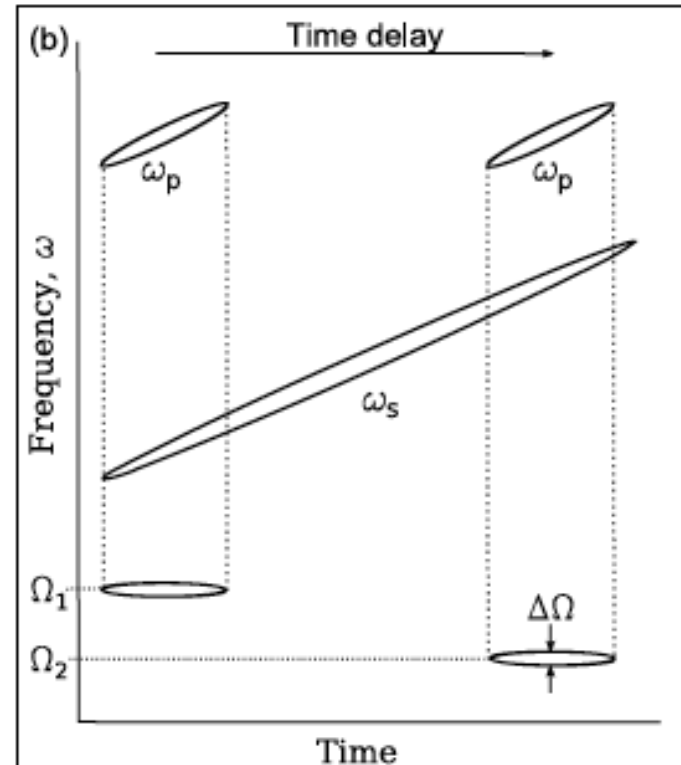
Conventional ps CARS



unmatched chirps fs CARS



Chirp matched fs CARS



The spectral resolution  $\Delta\Omega$  is determined by the total height of the ellipse  $\omega_p - \omega_s$ .