# Real-Time Absolute Frequency Measurement of CW-THz Radiation Based on a Free-Running THz Comb

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## Abstract

Absolute frequency of continuous-wave terahertz radiation was determined at an acuracy of  $10^{-11}$  in real time by modulating a frequency spacing of photocarrier terahertz comb induced by a free-running femtosecond laser.

### I. INTRODUCTION

measurement is Frequency the most basic measurement technology in the light and electric waves, but in THz region (wavelength =  $30 \sim 3000 \ \mu m$ , frequency =  $0.1 \sim 10$  THz) which has not been explored for a long time, it has been difficult to measure frequencies in THz region with high accuracy in a room temperature environment. Therefore, we have been researching THz-comb-referenced spectrum analyzer which enables high precision frequency measurement at room temperature environment by following the procedures described as below: First, generate photocarrier terahertz frequency comb (PC-THz comb) in photoconductive antenna (PCA). Second, mix CW-THz wave and the generated PC-THz comb. Finally, beat down the resultant signal to the RF region by photoconductive mixing [1, 2]. However, in these previous researches, it is necessary to measure beat frequencies before and after shifting comb interval (= repetition frequency) in order to determine the comb mode number that is nearest to the CW-THz wave. This temporally serial, two-step measurement has been an obstacle to the real-time measurement. Recently, the absolute frequency of fluctuating CW-THz wave has been determined by measuring two beat frequencies simultaneously using two PC-THz combs with different comb intervals [3]. However, the use of dual stabilized femtosecond lasers may hinder its wide use. In this paper, we report here that we realized high-speed absolute frequency measurement using a single, free-running, frequency-modulated PC-THz comb.

## **II. PRINCIPLE**

THz-comb-referenced spectrum analyzer is based on a heterodyne technique based on photoconductive mixing [1, 2]. Figure 1(a) shows the spectral behavior of PC-THz comb mode (freq. interval =  $f_{rep}$ ) and CW-THz radiation (freq. =  $f_{THz}$ ) in this method. When  $f_{rep}$  is modulated sinusoidally (maximum  $f_{rep}$  value =  $f_{rep\_max}$ , minimum  $f_{rep}$  value =  $f_{rep\_min}$ ),  $f_{beat}$  is also modulated in synchronization with the modulated  $f_{rep}$  (maximum  $f_{beat}$  value =  $f_{beat max}$ ,

minimum  $f_{beat}$  value =  $f_{beat\_min}$ ) as shown Fig. 1(b). If fluctuation of  $f_{THz}$  is much slower than modulation frequency of  $f_{rep}$ , the mode order *m* of PC-THz comb nearest in frequency to  $f_{THz}$  can be determined using the following equation.

$$m = (f_{beat\_max} - f_{beat\_min}) / (f_{rep\_max} - f_{rep\_min}).$$
(1)

Finally,  $f_{THz}$  is calculated as follow

$$f_{THz} = mf_{rep} - f_{beat} \qquad \langle \text{in - phase between } f_{rep} \text{ and } f_{beat} \rangle$$
(2)  
$$f_{THz} = mf_{rep} + f_{beat} \qquad \langle \text{out - of - phase between } f_{rep} \text{ and } f_{beat} \rangle$$

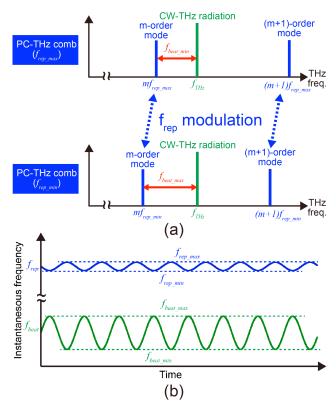


Fig. 1. Principle of operation.

## **III. EXPERIMENTAL SETUP**

Figure 2 shows an experimental setup of the proposed method. A femtosecond fiber laser (center wavelength = 1550 nm, pulse duration = 50 fs) was operated in freerunning condition around a repetition frequency of 100 MHz. Then  $f_{rep}$  is modulated sinusoidally at frequency of 100 Hz by changing the fiber cavity length with PZT. When a CW-THz radiation is incident onto a photoconductive antenna (PCA) for THz detection together with a  $f_{rep}$ -modulated laser beam, a beat signal between PC-THz comb mode and CW-THz radiation is generated from PCA as a current signal. The current beat signal was amplified by a current preamplifier. Temporal waveforms of the beat signal and the laser pulse signal are acquired at a sampling rate of 100 MHz by a fast digitizer. Instantaneous frequency values of them  $(f_{beat}$  and  $f_{rep})$  were obtained using a Hilbert transform [4].

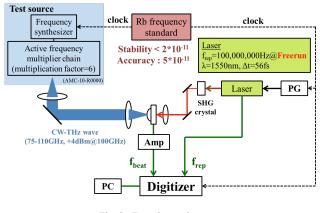


Fig. 2. Experimental setup

## **IV. RESULTS**

Figure 3(a) and 3(b) respectively show the temporal change of  $f_{rep}$  and  $f_{beat}$  when we used an active frequency multiplier chain (frequency range = 75~120 GHz, linewidth < 0.6 Hz,  $f_{THz}$  = 100.001,004 GHz) as a test source. From  $f_{beat\_max}$  = 998 kHz,  $f_{beat\_min}$  = 995 kHz,  $f_{rep\_max}$  = 100.000,009 MHz, and  $f_{rep\_min}$  = 100.000,006 MHz in Fig. 3(a), *m* was determined to be 1000. Finally, we confirmed that  $f_{THz}$  was fluctuated around 100.001,004 GHz as shown in Fig. 3(c). The determined  $f_{THz}$  coincided with the configured  $f_{THz}$  with accuracy of 10<sup>-11</sup>.

### V. CONCLUSIONS

We measured the absolute frequency of the CW-THz radiation with accuracy of  $10^{-11}$  in real time using a single, free-running,  $f_{rep}$ -modulated femtosecond laser. Although  $f_{rep}$  is actively modulated in this paper, the similar experiment will be performed using the natural walking of  $f_{rep}$  in the free-running laser.

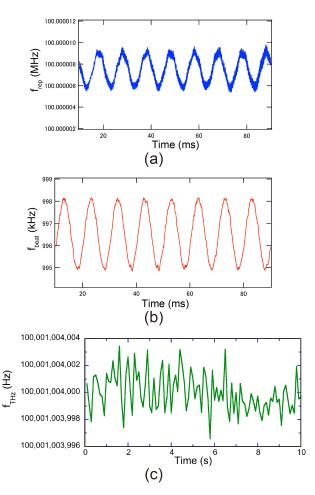


Fig. 3. Temporal change of (a)  $f_{rep}$ , (b)  $f_{beat}$ , and (c)  $f_{THz}$ .

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