

High-speed ellipsometer

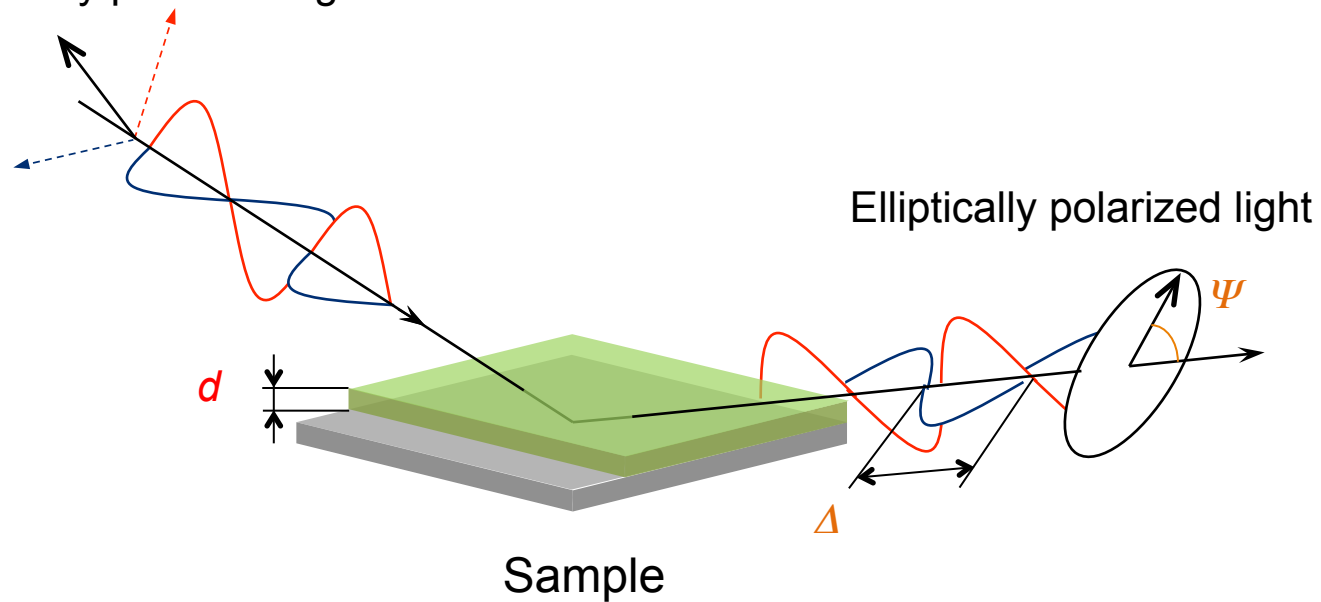
2015/06/11

PD Yi-Da Hsieh

Introduction

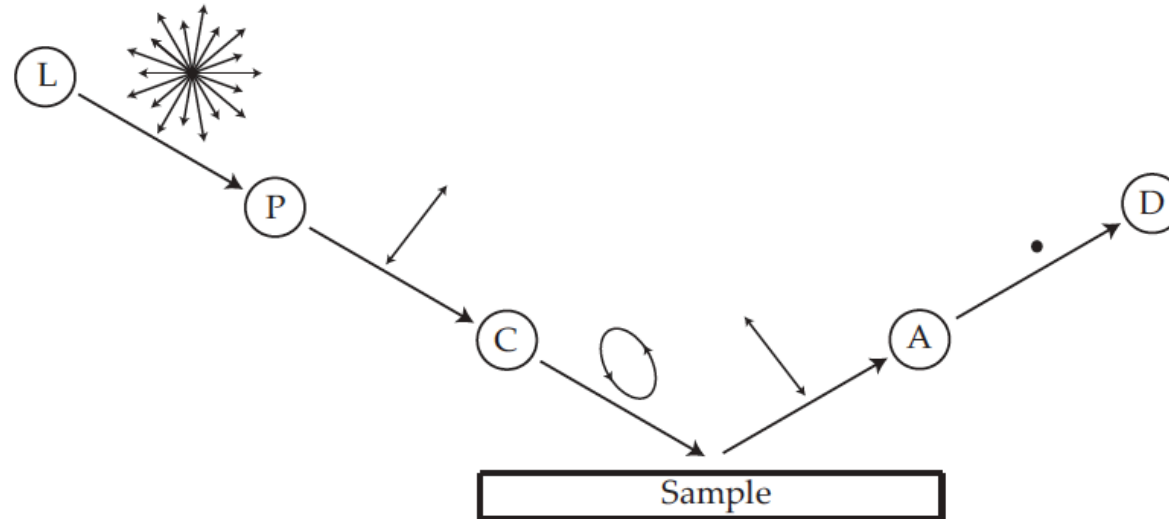
- Ellipsometer

45° Linearly polarized light

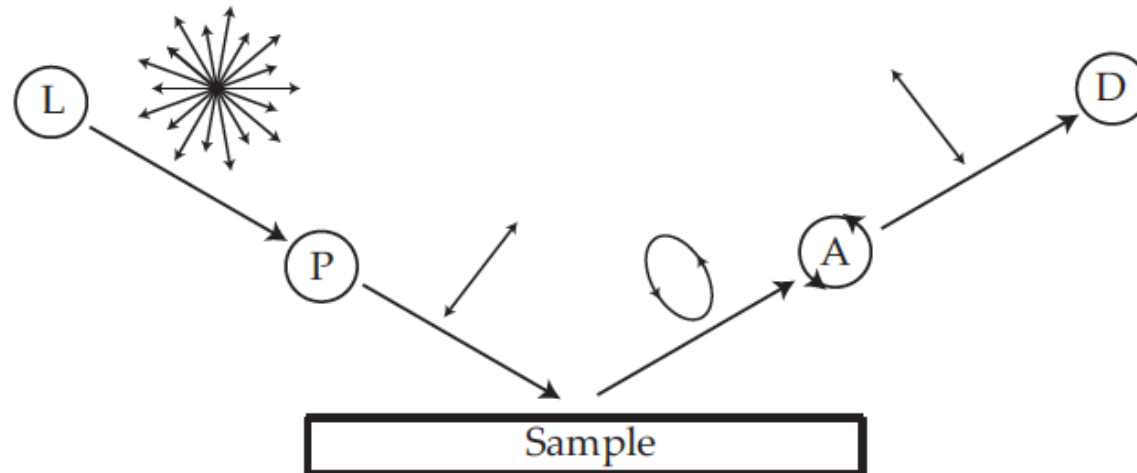


Introduction

- Null ellipsometer



- Photometric ellipsometer



- Determination of retardation parameters of multiple-order wave plate using a phase-sensitive heterodyne ellipsometer

Ref) C. -H. Hsieh, et. al., Appl. Opt. 46: 5944 (2007)

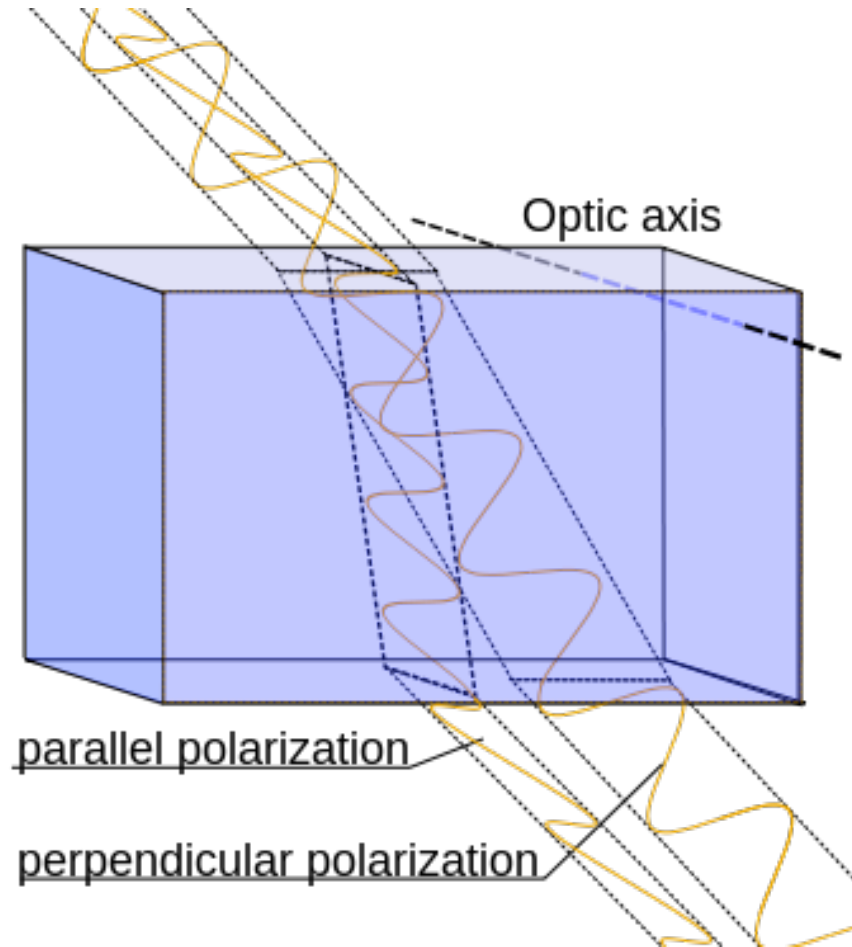
- High speed interferometric ellipsometer

Ref) C. -C. Tsai, et., al., Opt. Express. 16: 7778 (2008)

- Dual-frequency paired polarization phase shifting ellipsometer

Ref) C. -J. Yu., et., al., Opt. commun. 282:1516 (2009)

Birefringent material



$$\Delta n = n_e - n_o$$

Experimental setup

Mach-Zehnder interferometer

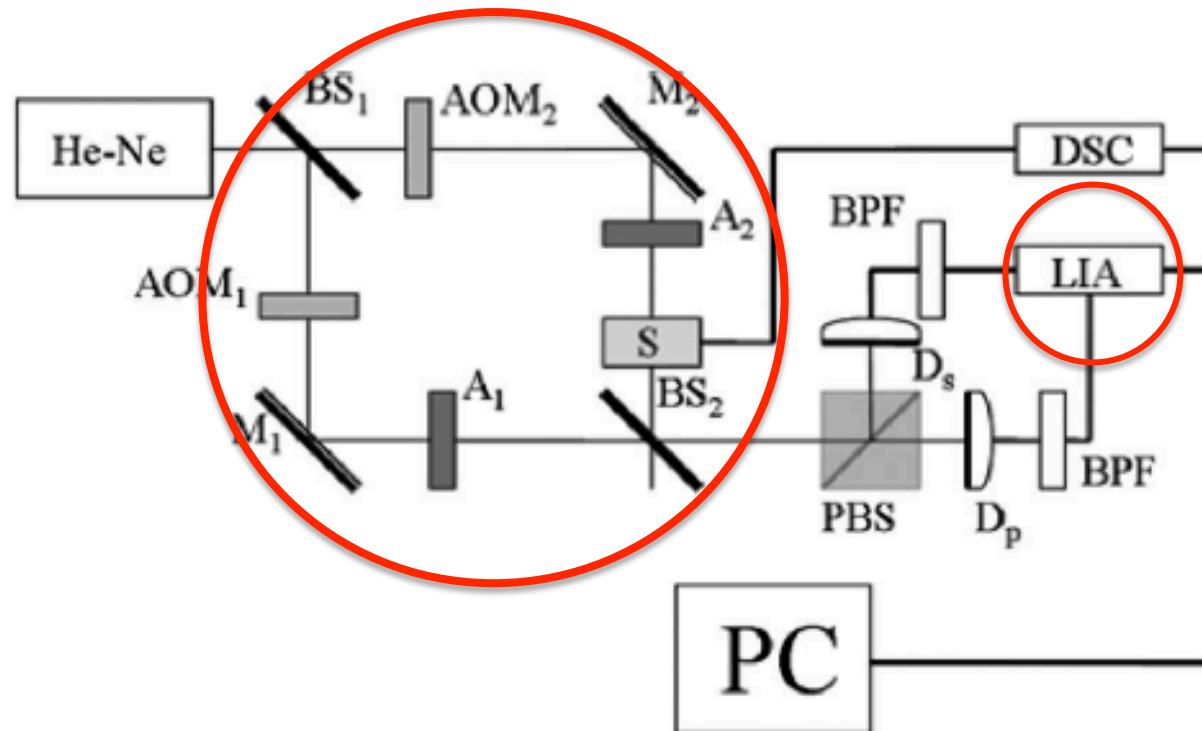
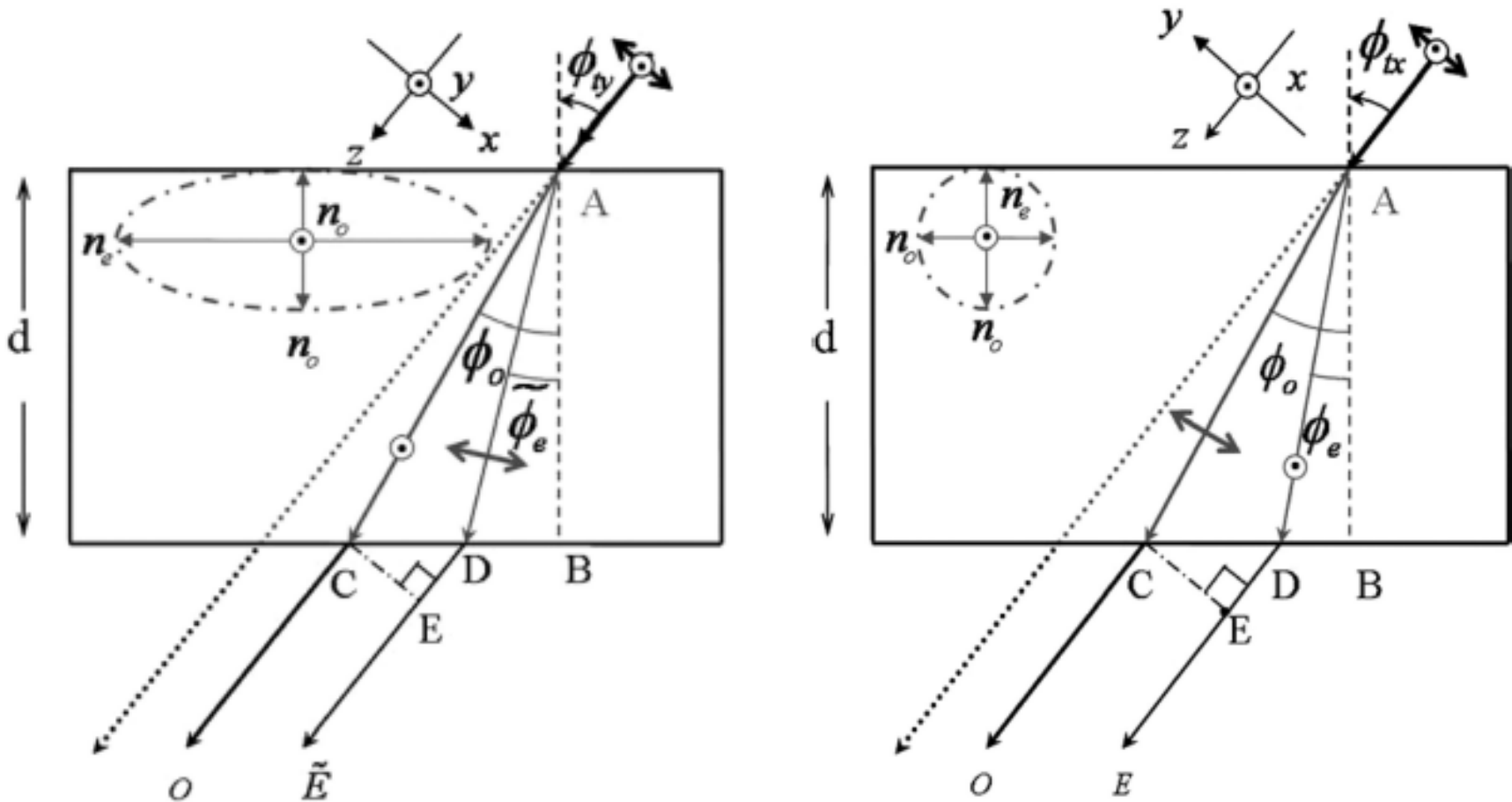


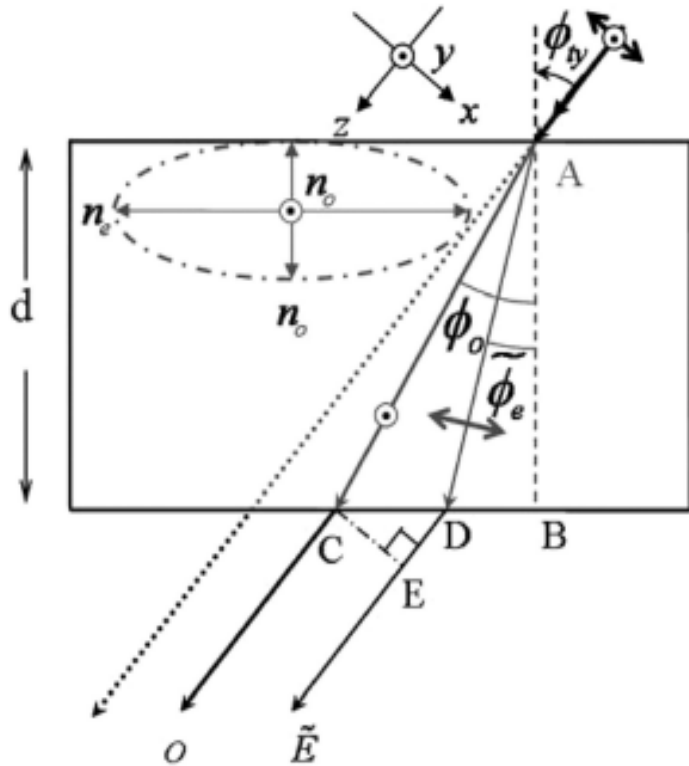
Fig. 1. Experimental setup: BS_1 , BS_2 : beam splitters, AOM_1 , AOM_2 : acousto-optic modulators, M_1 , M_2 : mirrors, A_1 , A_2 : analyzers, S : test sample on rotation stage, PBS : polarization beam splitter, D_p , D_s : photo detectors, BPF : band-pass filter, LIA : lock-in amplifier, DSC : digital stepping controller, PC : personal computer.

Method

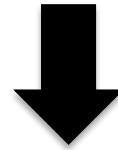
- Multiple-order wave plate
 - A linear birefringent material



Method

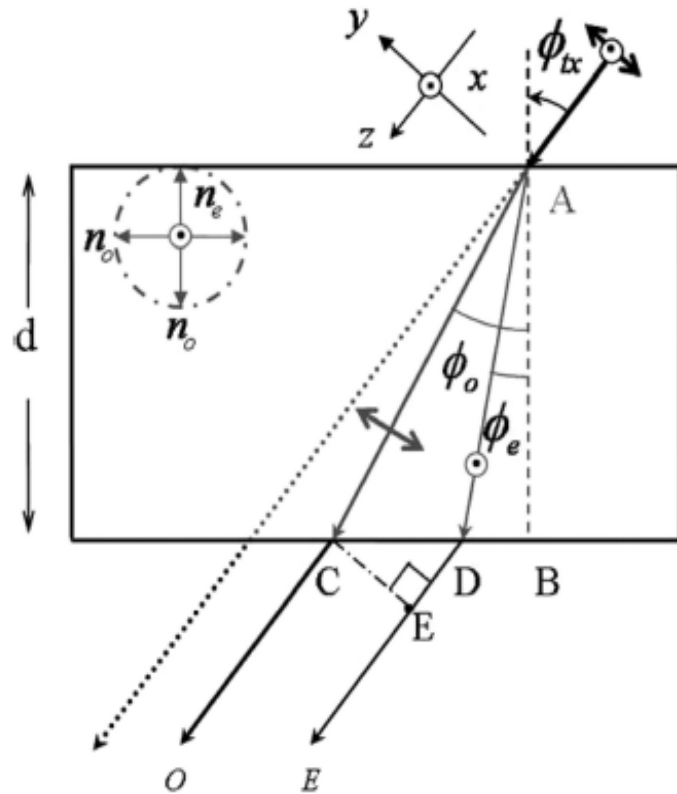


$$\begin{aligned}
 \delta_{ty} &= \delta_s - \delta_p \\
 &= \frac{2\pi}{\lambda} (n_o \overline{AC}) - \frac{2\pi}{\lambda} (\tilde{n}_e \overline{AD} + \overline{DE}) \\
 &= \frac{2\pi}{\lambda} d (n_o \cos \phi_o - \tilde{n}_e \cos \tilde{\phi}_e) \\
 &= \frac{2\pi}{\lambda} d \left(\sqrt{n_o^2 - \sin^2 \phi_{ty}} - \sqrt{n_e^2 - \frac{n_e^2}{n_o^2} \sin^2 \phi_{ty}} \right),
 \end{aligned}$$



$$\begin{aligned}
 \delta_{ty} - \delta_0 &= \frac{2\pi}{\lambda} d \left[\left(\sqrt{n_o^2 - \sin^2 \phi_{ty}} - \sqrt{n_e^2 - \frac{n_e^2}{n_o^2} \sin^2 \phi_{ty}} \right) \right. \\
 &\quad \left. - (n_o - n_e) \right], \tag{10}
 \end{aligned}$$

Method

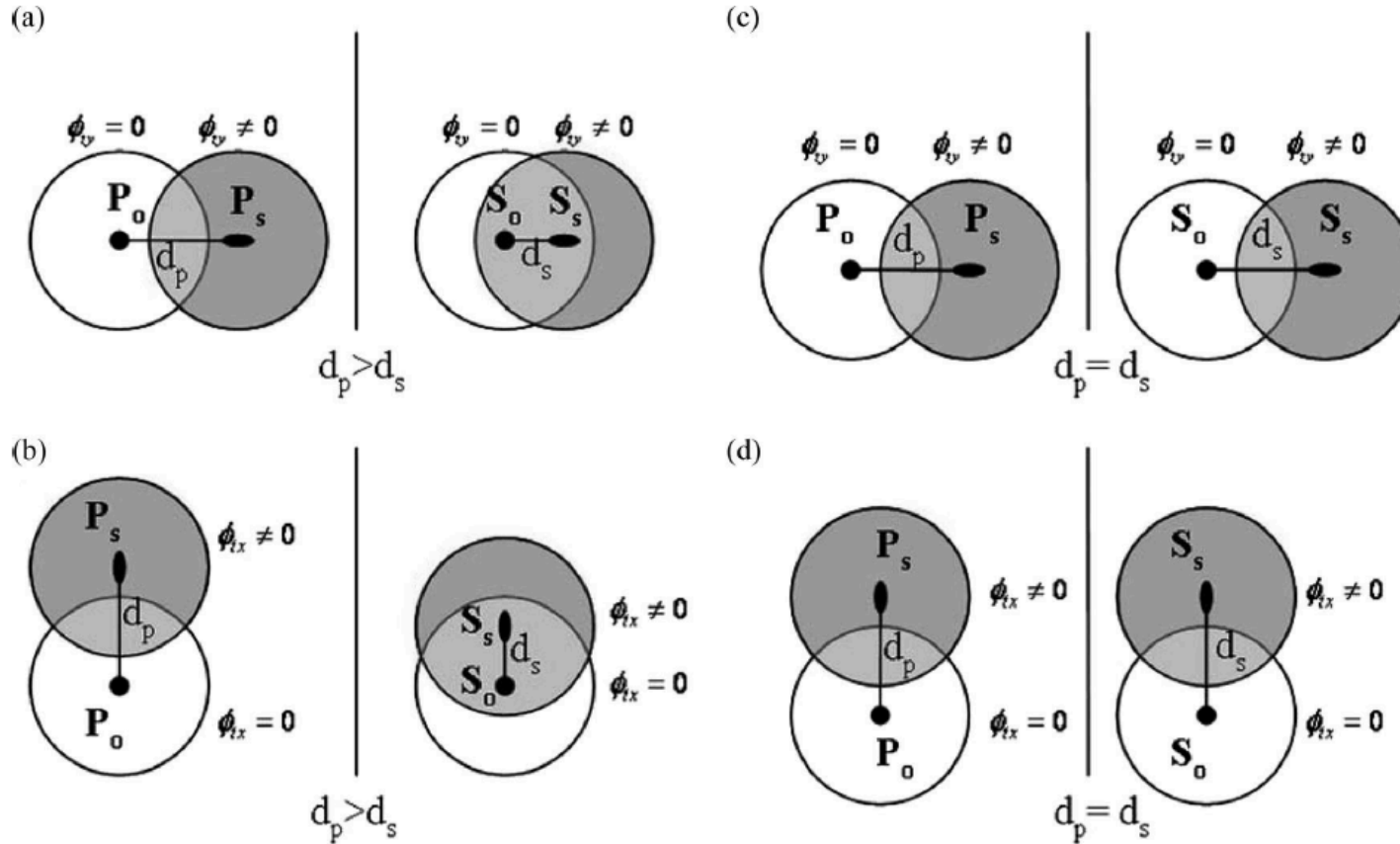


$$\delta_{tx} - \delta_0 = \frac{2\pi}{\lambda} d \left[\left(\sqrt{n_o^2 - \sin^2 \phi_{tx}} - \sqrt{n_e^2 - \sin^2 \phi_{tx}} \right) - (n_o - n_e) \right], \quad (11)$$

For a linearly birefringent medium :

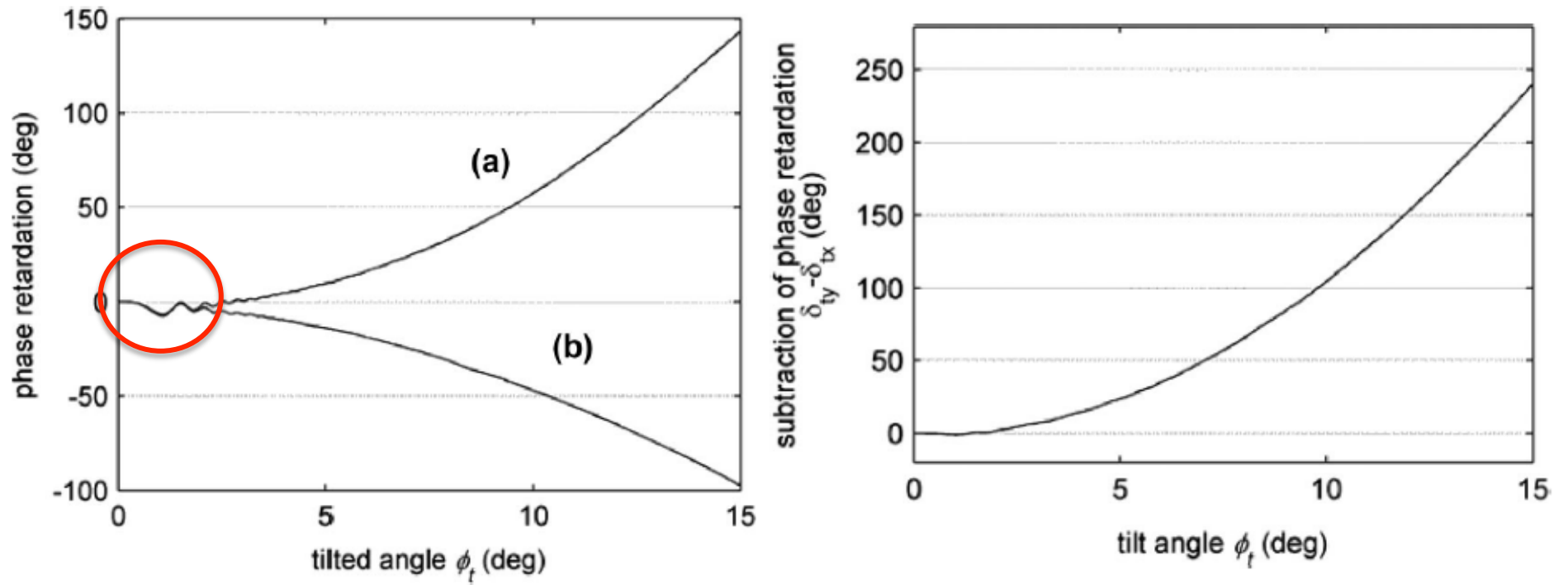
$$\frac{2\pi}{\lambda} d(n_e - n_o) = 2m\pi + \Gamma.$$

Method

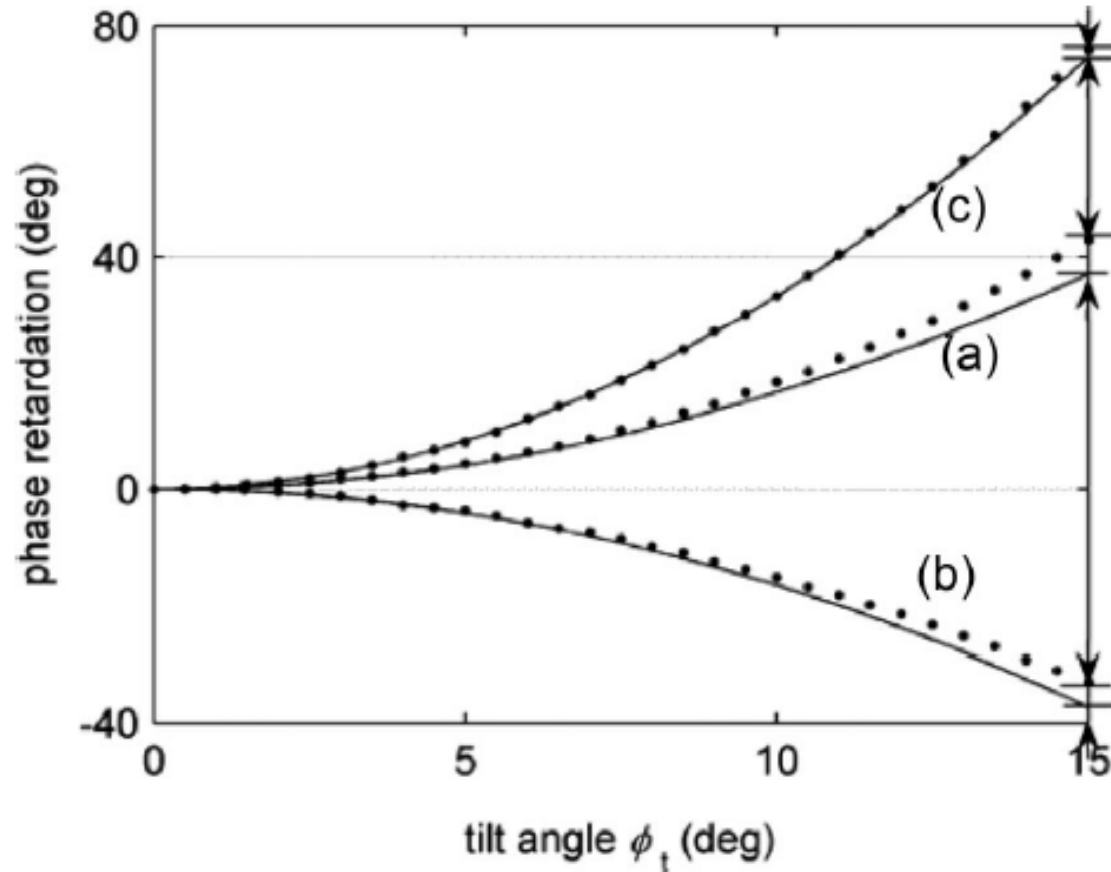


$$(\delta_{ty} - \delta_{tx}) / (2m\pi + \Gamma) = \left(\sqrt{n_e^2 - \sin^2 \phi_t} - \sqrt{n_e^2 - n_e^2 \sin^2 \phi_t / n_o^2} \right) / (n_e - n_o).$$

Results



Results



- $m=7$
- $n_o=1.5427$
- $n_e=1.5518$
- Error: 0.05%

Summary

- highly sensitive and accurate measurement of retardation parameters (RPs), which includes the refractive indices of the extraordinary ray n_e and ordinary ray n_o , is obtained by this method.

- Determination of retardation parameters of multiple-order wave plate using a phase-sensitive heterodyne ellipsometer

Ref) C. -H. Hsieh, et. al., Appl. Opt. 46: 5944 (2007)

- High speed interferometric ellipsometer

Ref) C. -C. Tsai, et., al., Opt. Express. 16: 7778 (2008)

- Dual-frequency paired polarization phase shifting ellipsometer

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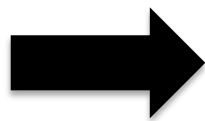
Method

- The polarized heterodyne signals at photo-detectors D_p and D_s can be expressed by

$$I_p(\delta\omega t) = A_{p1}^2 + A_{p2}^2 + 2A_{p1}A_{p2} \cos[\delta\omega t + \delta\phi_p],$$

$$I_s(\delta\omega t) = A_{s1}^2 + A_{s2}^2 + 2A_{s1}A_{s2} \cos[\delta\omega t + \delta\phi_s],$$

- set $\alpha = \delta\omega t + \frac{\delta\phi_s + \delta\phi_p}{2}$, $\beta = \frac{\delta\phi_s - \delta\phi_p}{2}$, $\kappa_p = 2A_{p1}A_{p2}$, and $\kappa_s = 2A_{s1}A_{s2}$



$$I_p(\delta\omega t) \equiv \kappa_p \cos[\alpha - \beta],$$

$$I_s(\delta\omega t) \equiv \kappa_s \cos[\alpha + \beta],$$

Method

- The output signal, from DA

$$\begin{aligned} I_{Diff}(\delta\omega t) &= I_S(\delta\omega t) - I_P(\delta\omega t) \\ &= (\kappa_S - \kappa_P) \cos \beta \cos \alpha - (\kappa_S + \kappa_P) \sin \beta \sin \alpha \\ &= \cos \gamma \cos \alpha - \sin \gamma \sin \alpha = \sqrt{\kappa_S^2 + \kappa_P^2 - 2\kappa_S \kappa_P \cos(\delta\phi_S - \delta\phi_P)} \cos(\alpha + \gamma) \\ &= \kappa_{Diff} \cos(\alpha + \gamma) \end{aligned}$$

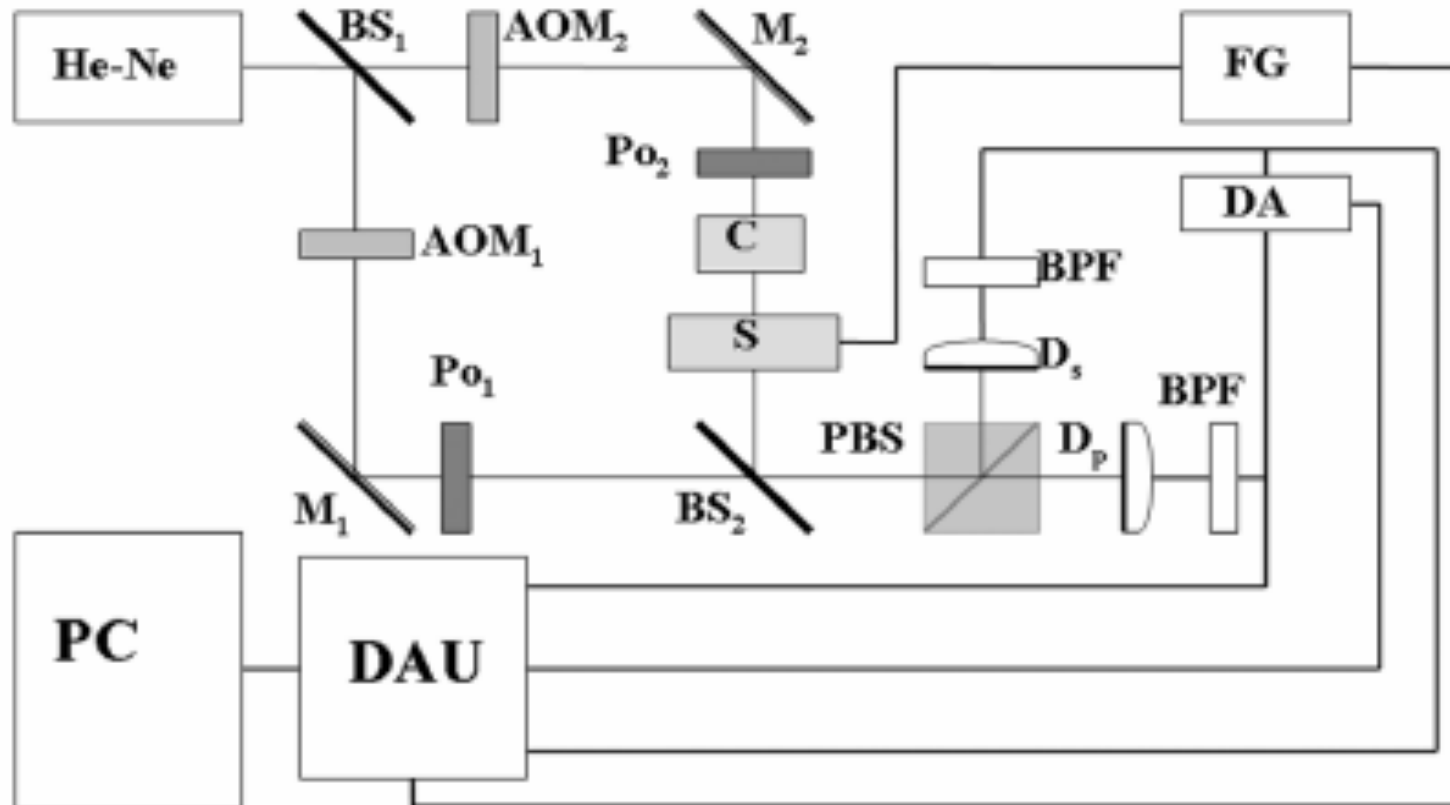
$$\kappa_{Diff} = \sqrt{\kappa_S^2 + \kappa_P^2 - 2\kappa_S \kappa_P \cos(\delta\phi_S - \delta\phi_P)}$$



$$\Delta = \cos^{-1} \left[\frac{\kappa_P^2 + \kappa_S^2 - \kappa_{Diff}^2}{2\kappa_P \kappa_S} \right],$$

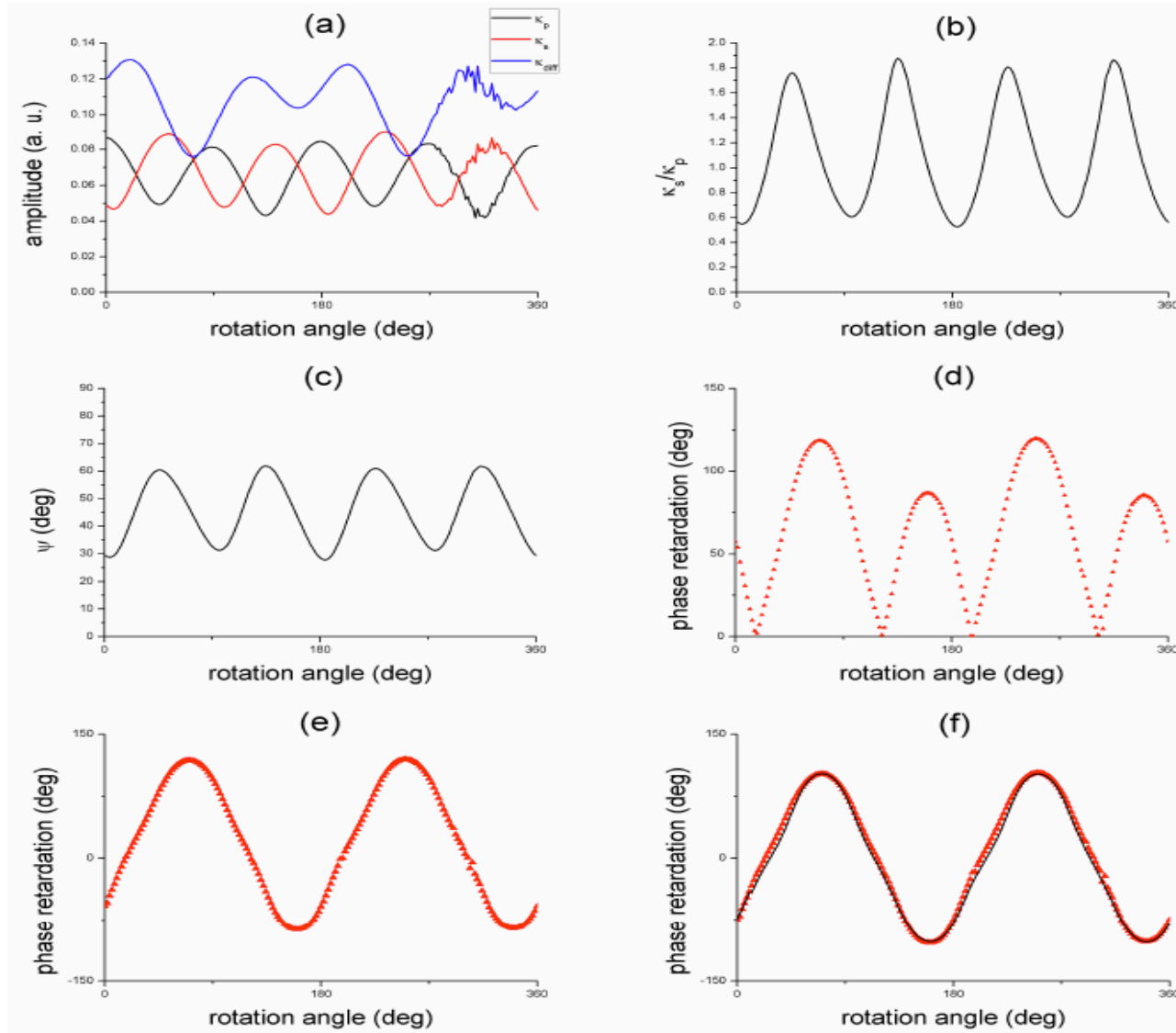
$$\psi = \tan^{-1} \left(\frac{\kappa_S}{\kappa_P} \right).$$

Experiment setup



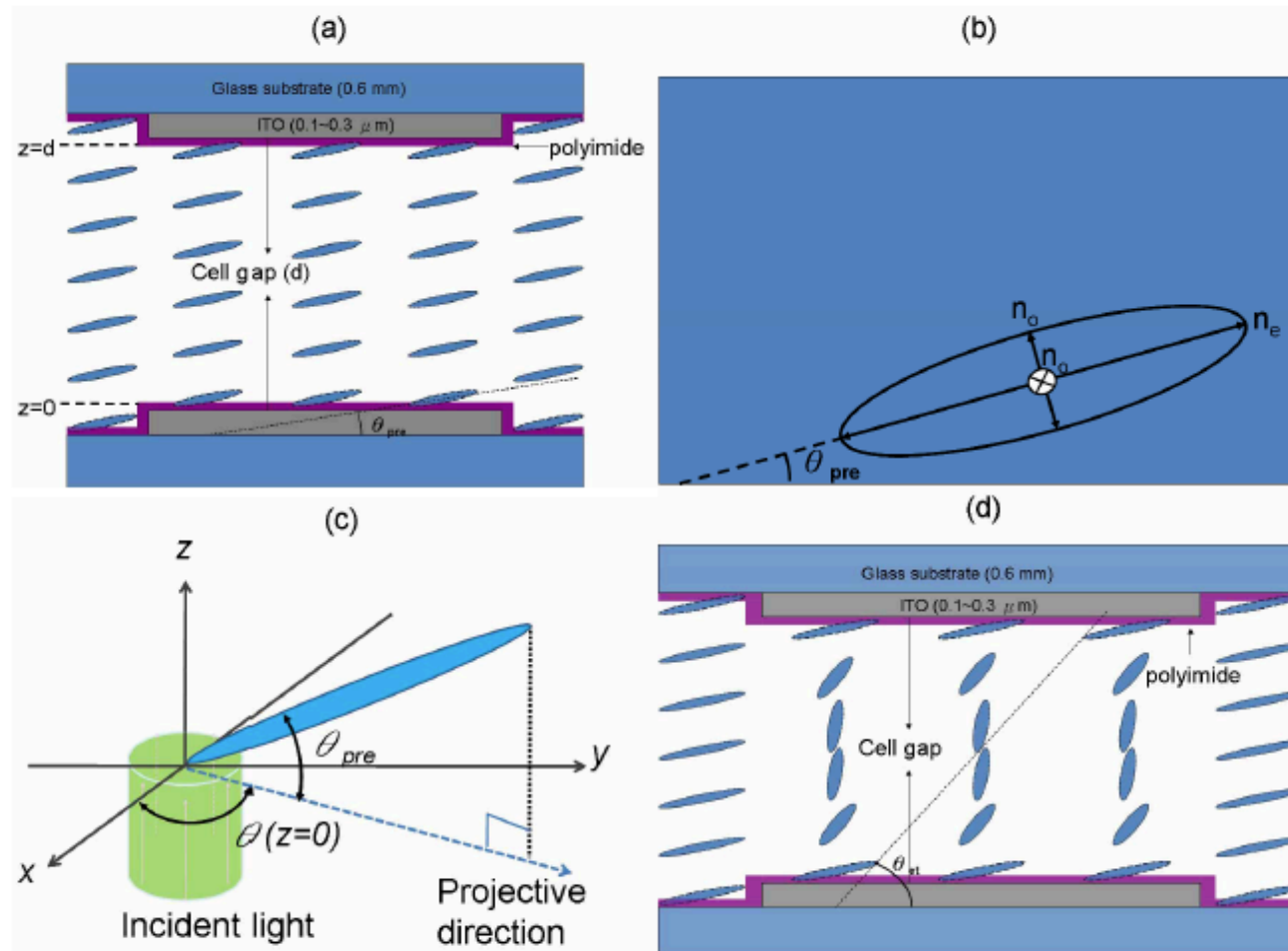
Results

Sample1: QWP

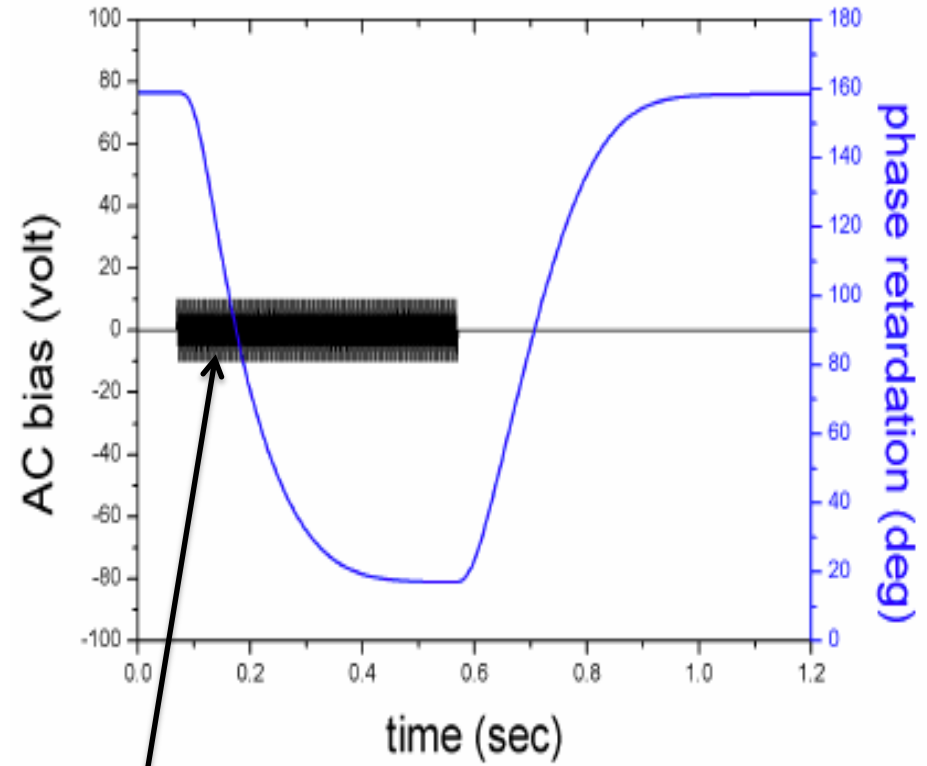
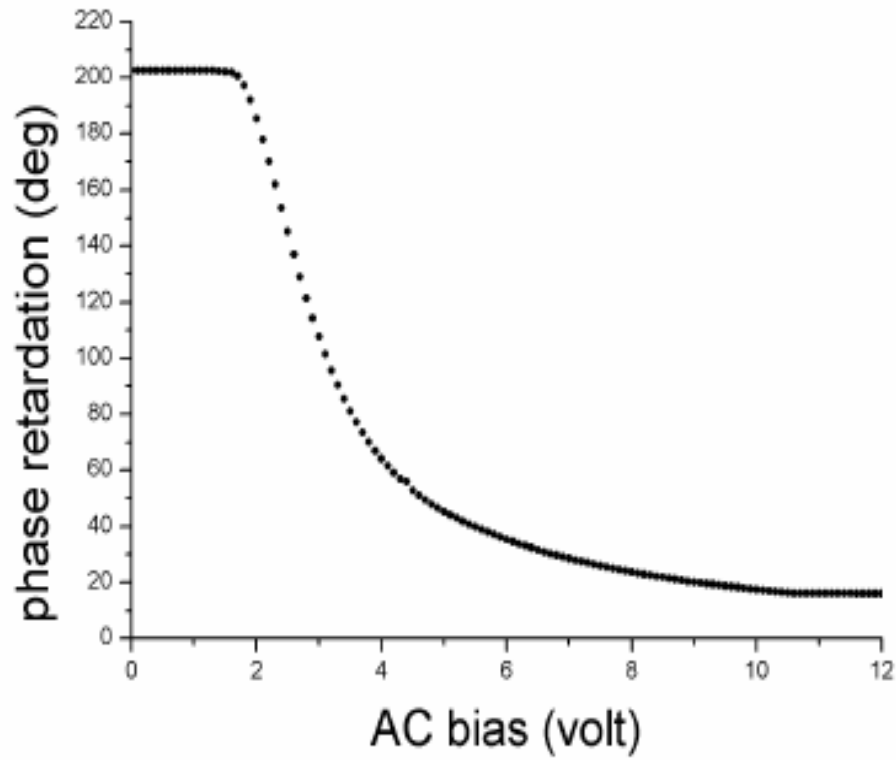


Results

Sample2: Parallel aligned liquid crystal device (PALCD)



Results



1kHz square wave

Summary

- high-speed interferometric ellipsometer not only able to measure ellipsometric parameters in real time but also to relax the requirement of equal amplitude of two polarized heterodyne signals.

- Determination of retardation parameters of multiple-order wave plate using a phase-sensitive heterodyne ellipsometer

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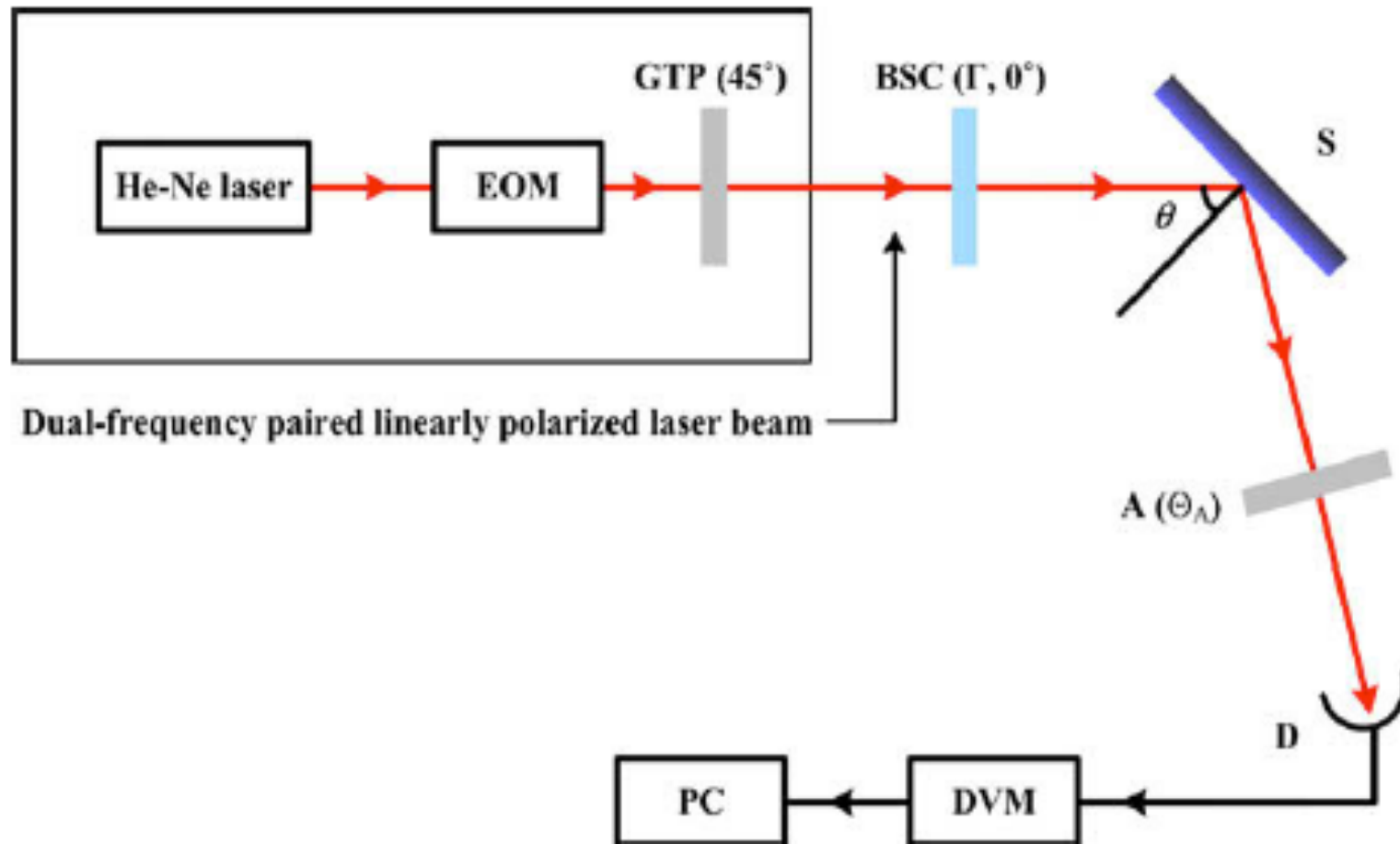
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Experiment setup



Dual frequency laser

- Linearly polarized light

$$\mathbf{E}_L = \frac{1}{\sqrt{2}} \begin{pmatrix} 1 \\ 1 \end{pmatrix} a \exp(i\omega_0 t)$$

- Applied a sawtooth wave for EOM

$$\Gamma = \frac{2\pi}{T}(t - mT) + \Gamma_0 + \frac{\pi}{V_\pi}(V_{\text{bias}} - V_\pi) = \omega t - 2m\pi + \Gamma_{\text{bias}},$$

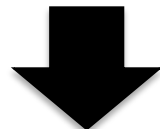
$$\Gamma_{\text{bias}} = \Gamma_0 + \frac{\pi}{V_\pi}(V_{\text{bias}} - V_\pi), \quad \longrightarrow \quad 0$$

Dual frequency laser

- With sawtooth wave

$$\Gamma = \omega t - 2m\pi$$

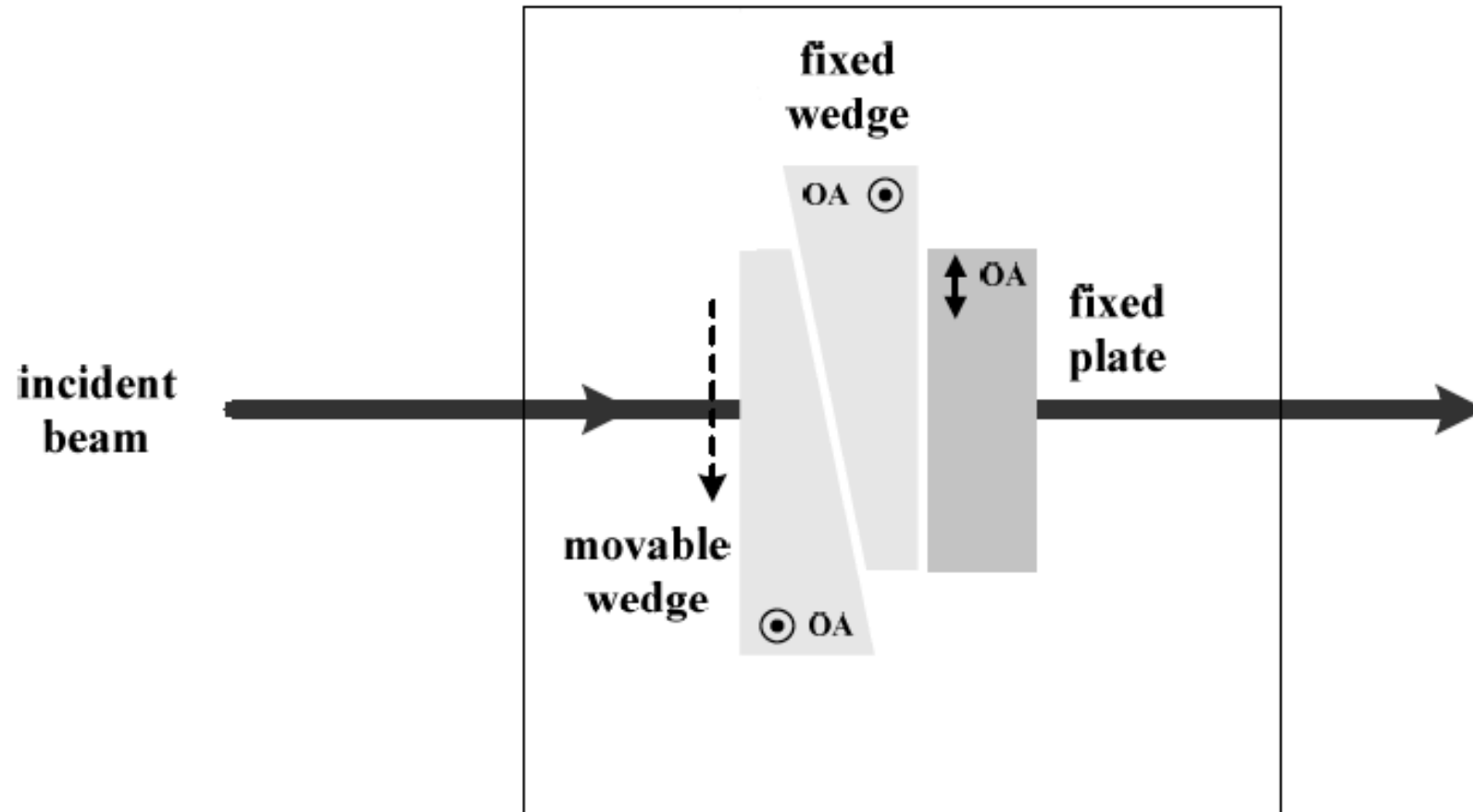
$$\mathbf{J}_{\text{EOM}}(\omega t) = \exp(-im\pi) \begin{pmatrix} \exp(i\omega t/2) & 0 \\ 0 & \exp(-i\omega t/2) \end{pmatrix}$$



$$\mathbf{E}_p = \frac{a}{\sqrt{2}} \begin{pmatrix} 1 \\ 0 \end{pmatrix} \exp(i\omega_p t) = \frac{a}{\sqrt{2}} \begin{pmatrix} 1 \\ 0 \end{pmatrix} \exp\left[i\left(\omega_0 + \frac{\omega}{2}\right)t\right],$$

$$\mathbf{E}_s = \frac{a}{\sqrt{2}} \begin{pmatrix} 0 \\ 1 \end{pmatrix} \exp(i\omega_s t) = \frac{a}{\sqrt{2}} \begin{pmatrix} 0 \\ 1 \end{pmatrix} \exp\left[i\left(\omega_0 - \frac{\omega}{2}\right)t\right].$$

Babinet Soleil compensator (BSC)



Method

- The Mueller matrices of BSC and analyzer are expressed as

$$\mathbf{M}_{\text{BSC}} = T_{\text{BSC}} \begin{pmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & \cos \Gamma & \sin \Gamma \\ 0 & 0 & -\sin \Gamma & \cos \Gamma \end{pmatrix},$$

$$\mathbf{M}_{\text{A}} = T_{\text{A}} \begin{pmatrix} 1 & \cos 2\theta_{\text{A}} & \sin 2\theta_{\text{A}} & 0 \\ \cos 2\theta_{\text{A}} & \cos^2 2\theta_{\text{A}} & \sin 2\theta_{\text{A}} \cos 2\theta_{\text{A}} & 0 \\ \sin 2\theta_{\text{A}} & \sin 2\theta_{\text{A}} \cos 2\theta_{\text{A}} & \sin^2 2\theta_{\text{A}} & 0 \\ 0 & 0 & 0 & 0 \end{pmatrix}.$$

- A dual-frequency paired linearly polarized laser beam, which can be expressed by Stokes vector as: $\mathbf{S}_{\text{DL}} = (1 \ 0 \ 1 \ 0)^T I_0 (1 + \cos \omega t)$

$$\mathbf{S}_{\text{out}} = \mathbf{M}_{\text{A}} \mathbf{M}_{\text{S}} \mathbf{M}_{\text{BSC}} \mathbf{S}_{\text{DL}}, \quad \Rightarrow \quad \tilde{I} = \pi_0 [1 - \cos 2\psi \cos 2\theta_{\text{A}} + \sin 2\psi \cos(\Delta + \Gamma) \sin 2\theta_{\text{A}}],$$

Method

- If Γ of BSC is adjusted at 0° and Θ_A is set either at 0° or 90° then:

$$\tilde{I}_p = 2\pi_0 \sin^2 \psi, \quad \text{at } \Theta_A = 0^\circ,$$

$$\tilde{I}_s = 2\pi_0 \cos^2 \psi, \quad \text{at } \Theta_A = 90^\circ,$$

and

$$\psi = \tan^{-1} \left(\tilde{I}_p / \tilde{I}_s \right)^{1/2}.$$

Method

- Similarly, when the analyzer is set at 45°

$$\tilde{I}_{45^\circ} = T_0 I_0 [1 + \sin 2\psi \cos(\Delta + \Gamma)],$$

- Thus, Δ can be obtained by shifting the phase retardation Γ of BSC at $0, 90, 180,$ and 270 sequentially.

$$\tilde{I}_1 = T_0 I_0 (1 + \sin 2\psi \cos \Delta), \quad \text{at } \Gamma = 0^\circ,$$

$$\tilde{I}_2 = T_0 I_0 (1 - \sin 2\psi \sin \Delta), \quad \text{at } \Gamma = 90^\circ,$$

$$\tilde{I}_3 = T_0 I_0 (1 - \sin 2\psi \cos \Delta), \quad \text{at } \Gamma = 180^\circ,$$

$$\tilde{I}_4 = T_0 I_0 (1 + \sin 2\psi \sin \Delta), \quad \text{at } \Gamma = 270^\circ.$$

$$\alpha = \frac{\tilde{I}_1 - \tilde{I}_3}{\tilde{I}_1 + \tilde{I}_3} = \sin 2\psi \cos \Delta,$$
$$\beta = \frac{\tilde{I}_4 - \tilde{I}_2}{\tilde{I}_4 + \tilde{I}_2} = \sin 2\psi \sin \Delta,$$

$$\Rightarrow \Delta = \tan^{-1}(\beta/\alpha).$$

Results

- The calibrated step wafer in which the silicon dioxide thin film (Mikropack ID0153).

Area	Ellipsometric parameters		Thickness
	ψ (°)	Δ (°)	T (nm)
#3: Measured	11.14	162.42	290.95
#3: Calibrated	10.83	162.23	290.16
#4: Measured	38.93	280.26	187.96
#4: Calibrated	38.30	280.06	189.20

Summary

- The phase shifting technique integrated into DPPSE fully expands the dynamic range of EP. This overcomes the limitation of conventional ellipsometer based on intensity modulation in measurement